

## 2. Image Enhancement

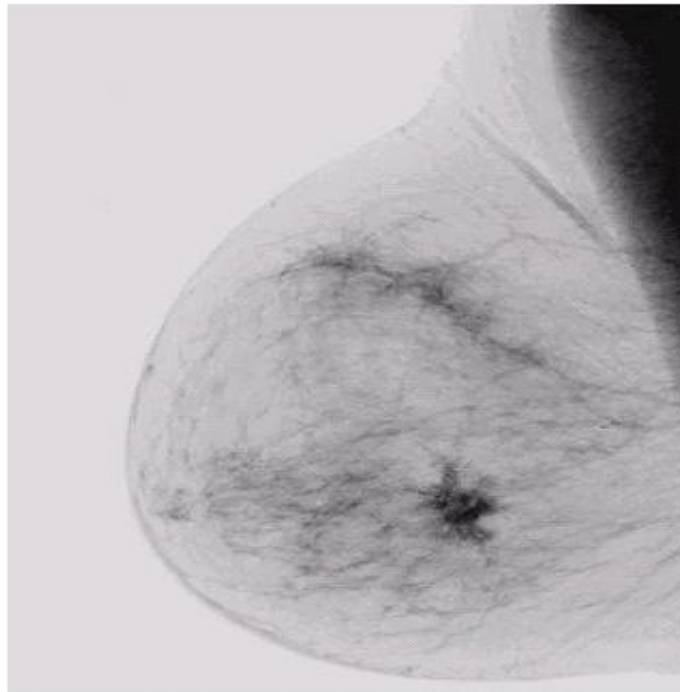
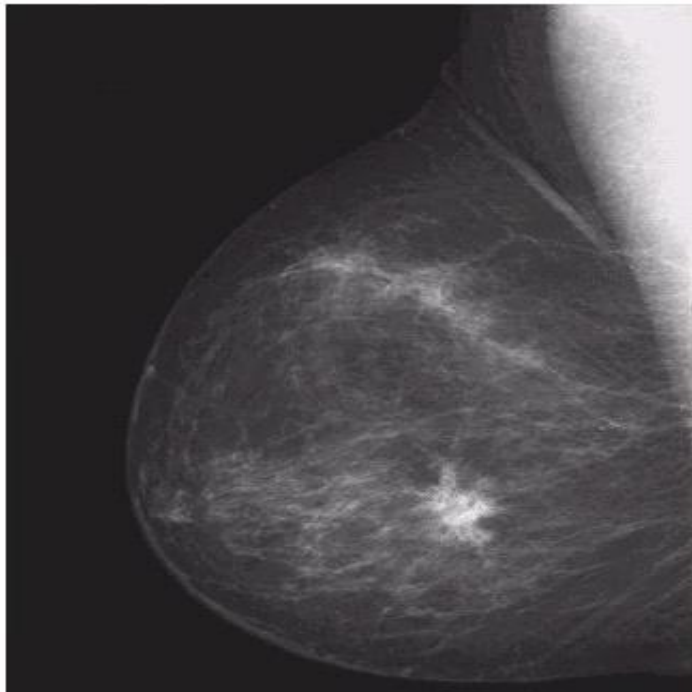
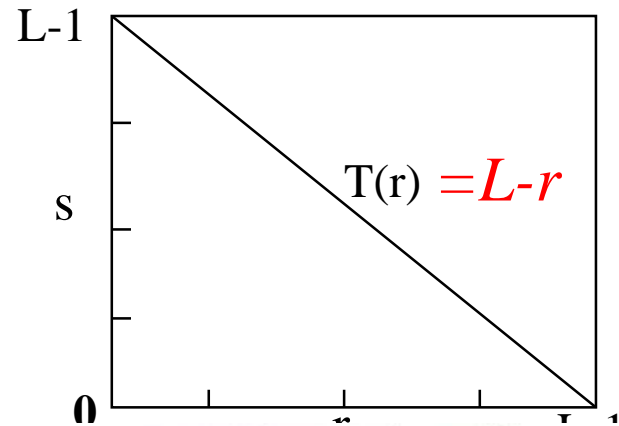
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The aim of image enhancement is to improve the **interpretability or perception** of information in images for human viewers, or to provide `better' input for other automated image processing techniques. Image enhancement techniques can be divided into two broad categories:

- **Spatial** domain methods, which operate directly on pixels, and
  - **Frequency** domain methods, which operate on the Fourier transform of an image.
- 
- Chapter 3 (Image Enhancement in the Spatial Domain)
  - Section 6.3 (Pseudocolor Image Processing)

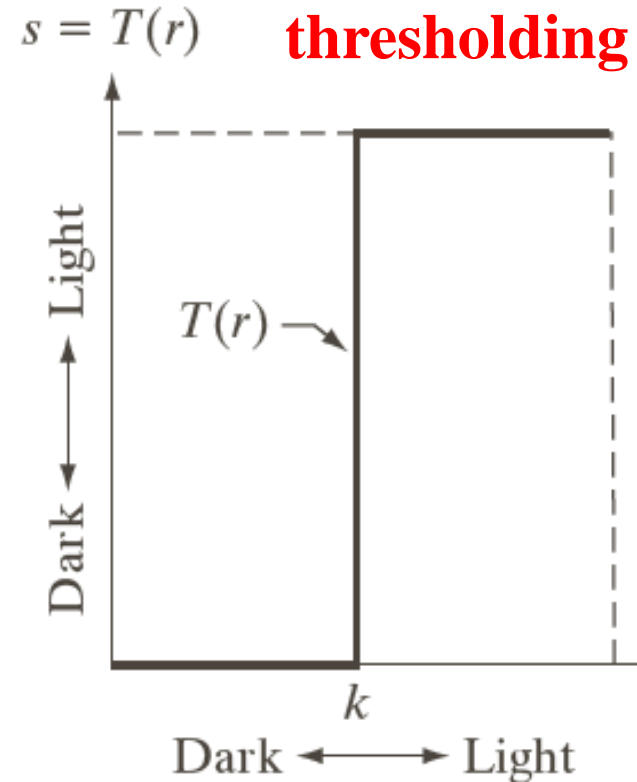
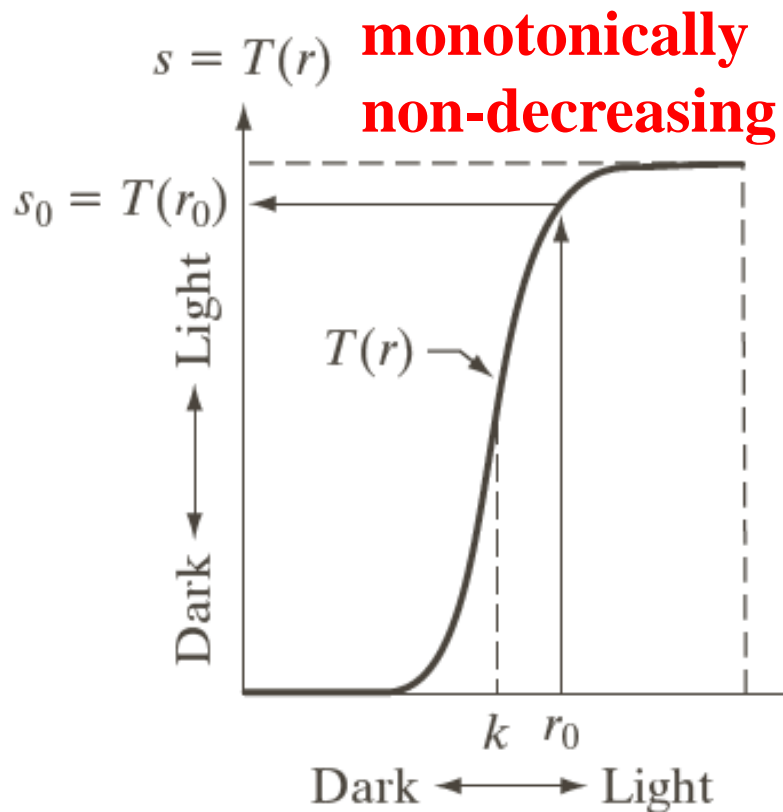
# Gray Level Transformations: Negative

- **Image Negative:** reverse the brightness from “black” to “white”. Useful in displaying medical images.



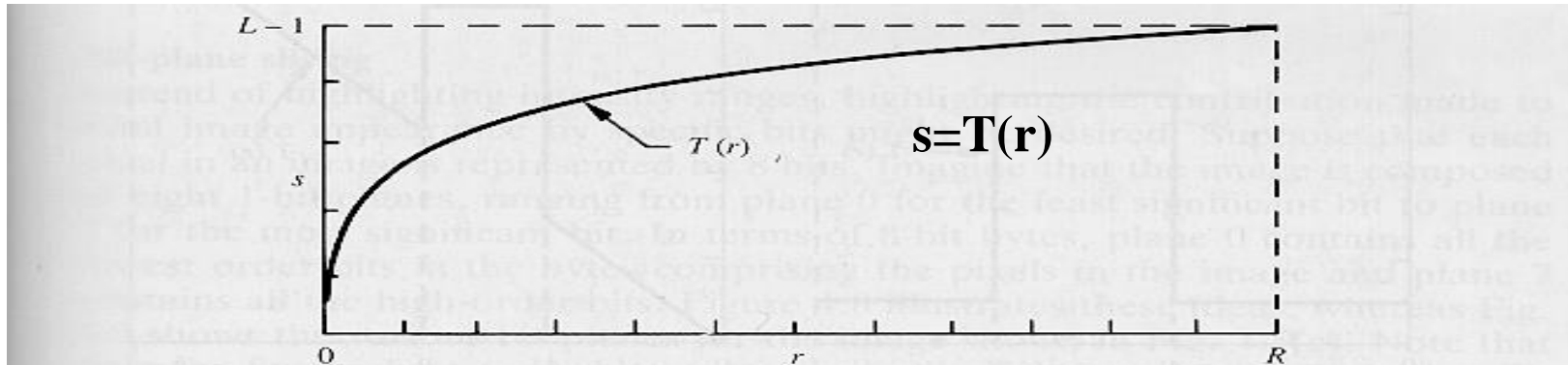
**FIGURE 3.4**  
(a) Original digital mammogram.  
(b) Negative image obtained using the negative transformation in Eq. (3.2-1).  
(Courtesy of G.E. Medical Systems.)

# Gray Level Transformation



# Gray Level Transformations: Dynamic Range Compression

- Processing images exceeding the display capability  $s = c \log(1 + |r|)$

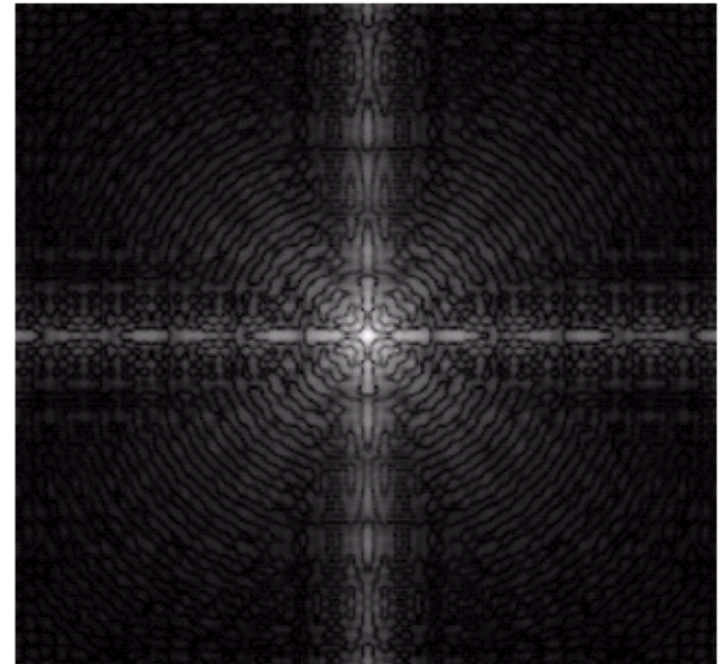
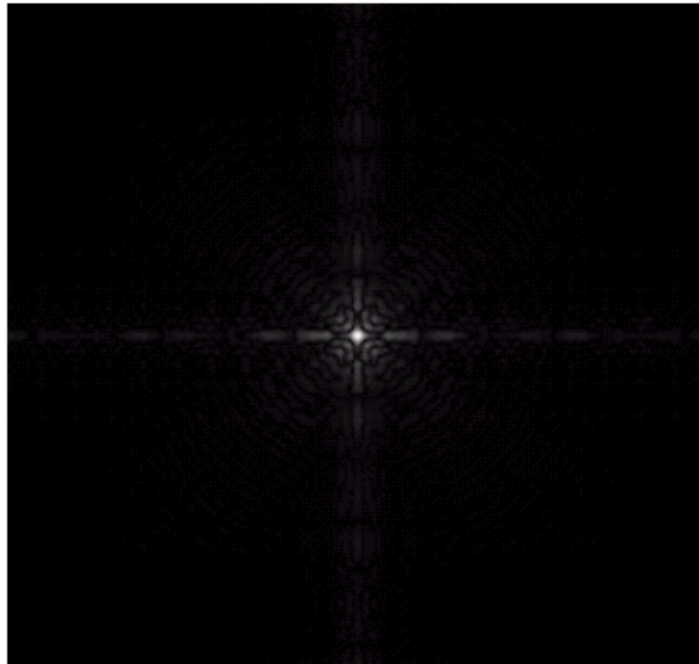


a b

**FIGURE 3.5**

(a) Fourier spectrum.

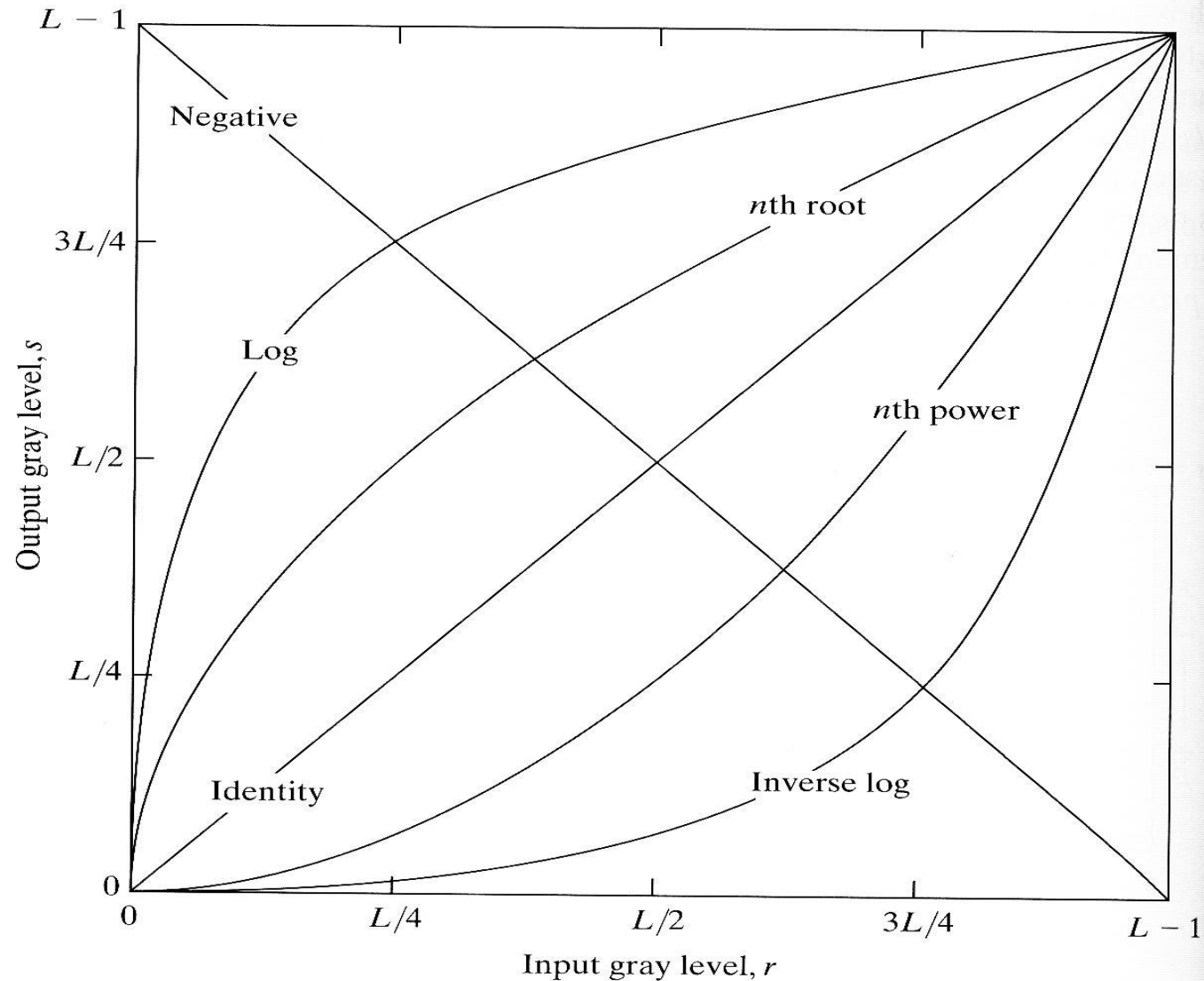
(b) Result of applying the log transformation given in Eq. (3.2-2) with  $c = 1$ .



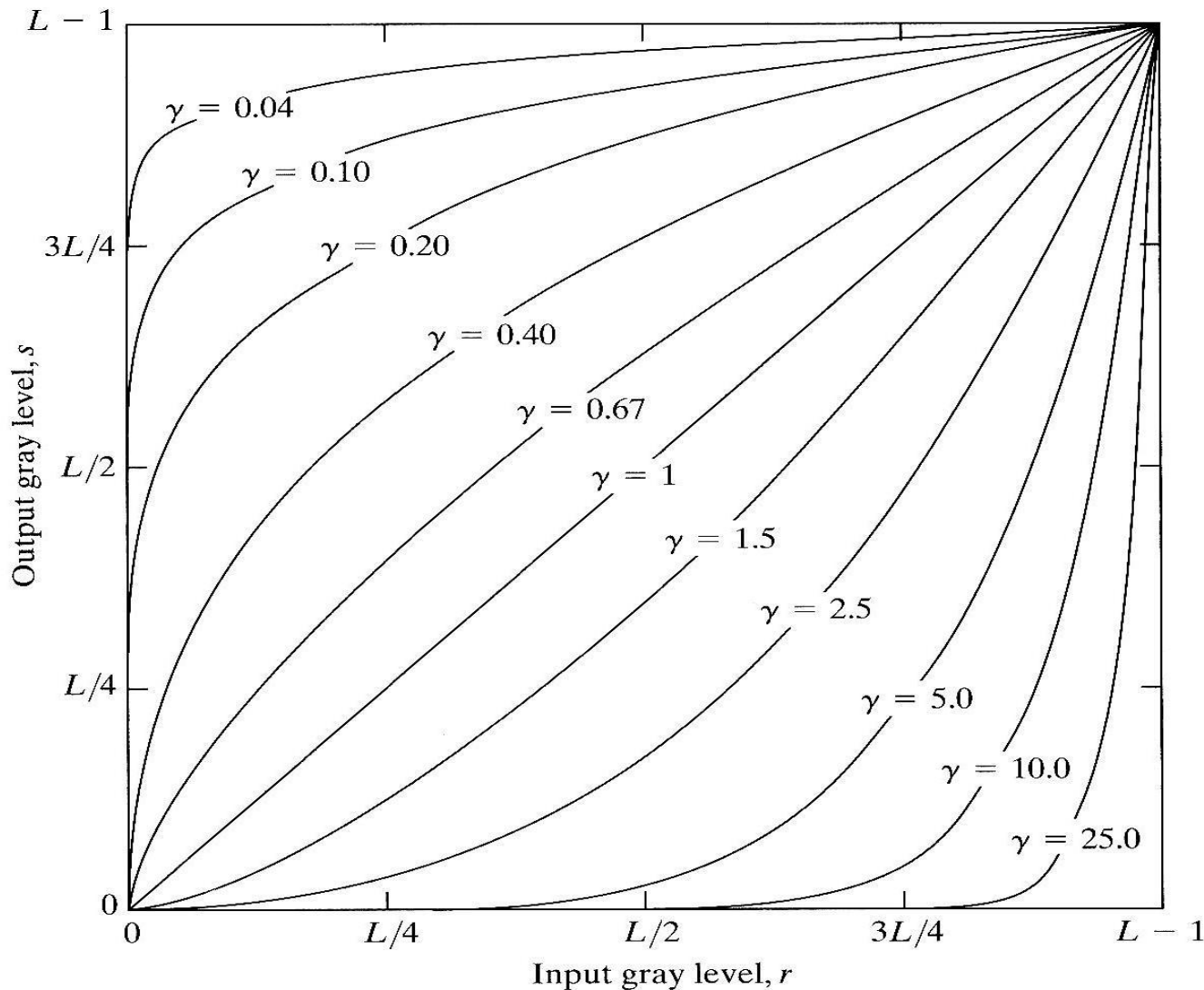


# Image Enhancement by Gray Level Transformations

**FIGURE 3.3** Some basic gray-level transformation functions used for image enhancement.



# Gray Level Transformations: Power-Law Transforms



**FIGURE 3.6** Plots of the equation  $s = cr^\gamma$  for various values of  $\gamma$  ( $c = 1$  in all cases).

$$s = T(r)$$
$$= cr^\gamma$$



# Gray Level Transformations: Power-Law Transforms

a b  
c d

**FIGURE 3.9**

(a) Aerial image.  
(b)–(d) Results of  
applying the  
transformation in  
Eq. (3.2-3) with  
 $c = 1$  and  
 $\gamma = 3.0, 4.0,$  and  
 $5.0$ , respectively.  
(Original image  
for this example  
courtesy of  
NASA.)







a	b
c	d

### FIGURE 3.8

(a) Magnetic resonance image (MRI) of a fractured human spine.

(b)–(d) Results of applying the transformation in Eq. (3.2-3) with  $c = 1$  and  $\gamma = 0.6, 0.4$ , and  $0.3$ , respectively.

(Original image courtesy of Dr. David R. Pickens, Department of Radiology and Radiological Sciences, Vanderbilt University Medical Center.)

# Gamma Correction on Monitors

a b  
c d

**FIGURE 3.7**

(a) Linear-wedge gray-scale image.  
(b) Response of monitor to linear wedge.  
(c) Gamma-corrected wedge.  
(d) Output of monitor.

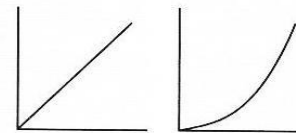
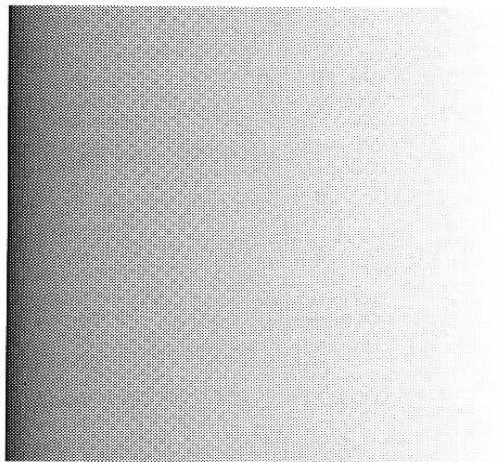
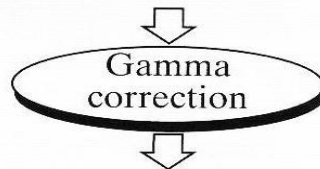
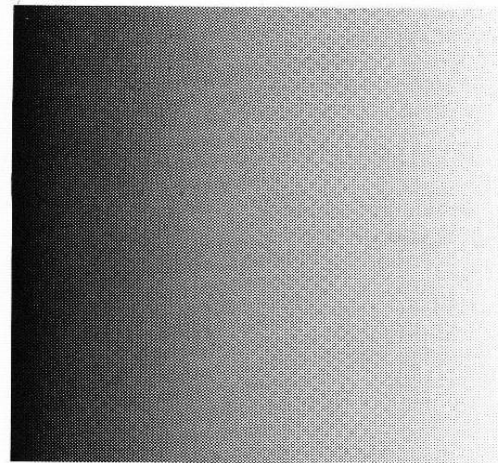


Image as viewed on monitor

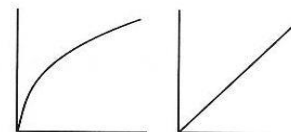
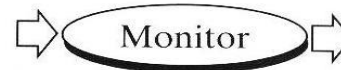
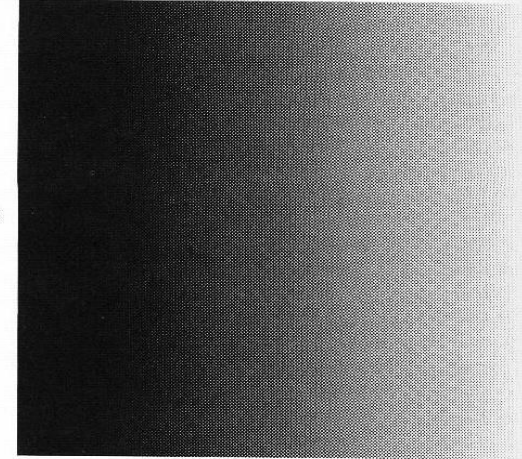
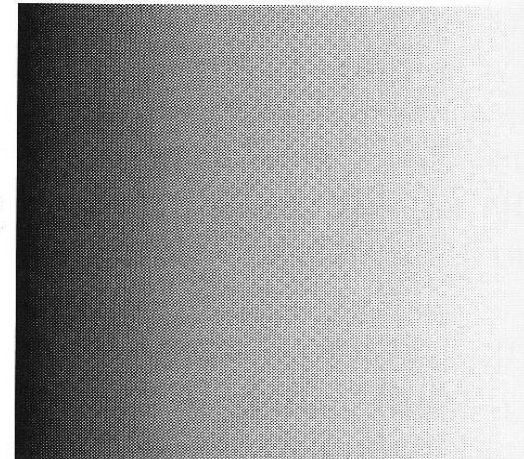


Image as viewed on monitor



$$s = r^{0.4}$$



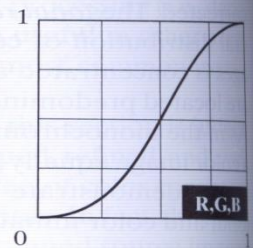
# Tonal Corrections for flat, light, and dark RGB color images



Flat



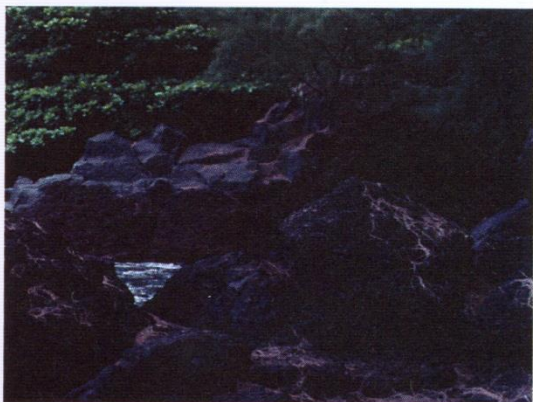
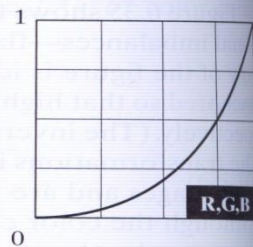
Corrected



Light



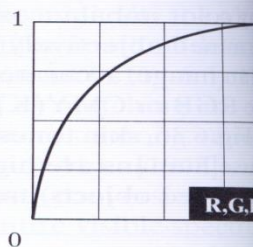
Corrected



Dark



Corrected



**FIGURE 6.35** Tonal corrections for flat, light (high key), and dark (low key) color images. Adjusting the red, green, and blue components equally does not alter the image hues.

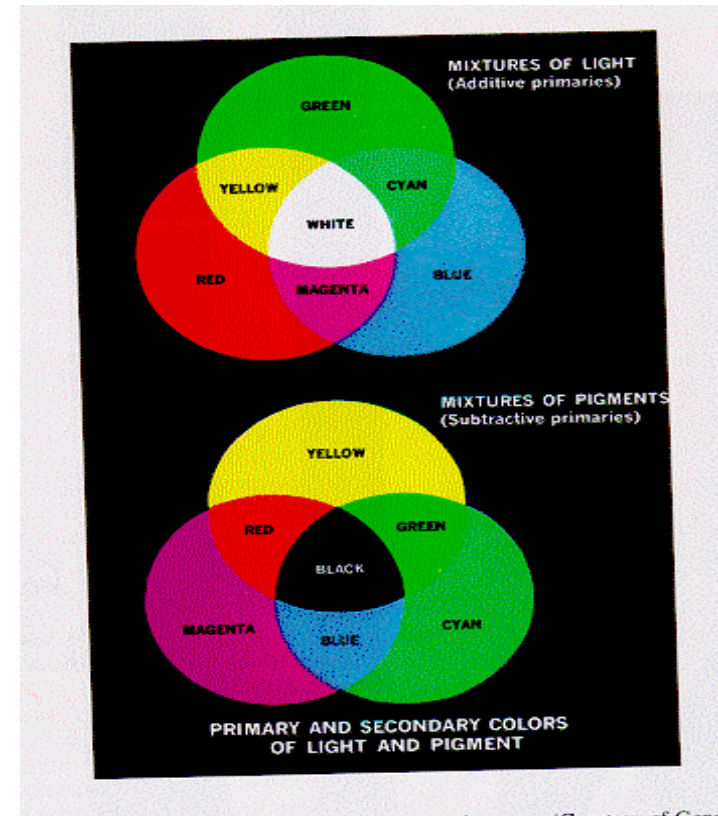
# CMYK Color System

- Cyan (255,0,0), Magenta (0,255,0), Yellow (0,0,255), Red (255,255,0), Green (255,0,255), Blue (255,255,0), etc.
- A practical variant, CMYK (with **K standing for “black”**), is spawned to provide an inexpensive ink. It is called 4-color printing.

**K**

$$\begin{matrix} \text{cyan} \\ \text{magenta} \\ \text{yellow} \end{matrix} \begin{bmatrix} C \\ M \\ Y \end{bmatrix} = \begin{bmatrix} 1 \\ 1 \\ 1 \end{bmatrix} - \begin{bmatrix} R \\ G \\ B \end{bmatrix}$$

(assume all color values have been normalized to the range [0,1])

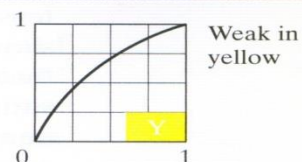
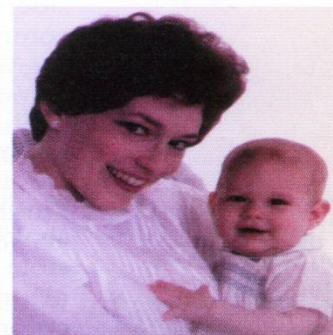
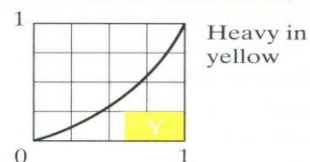
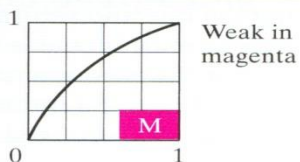
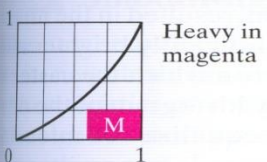
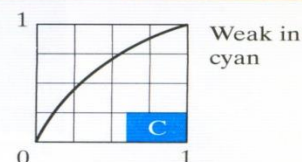
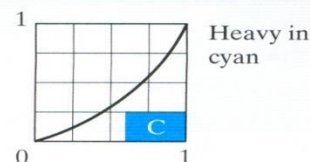
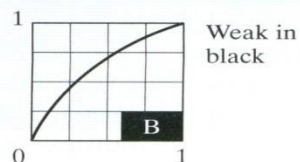
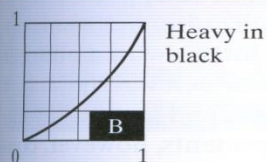




# Color Balancing Corrections for CMYK Color Images



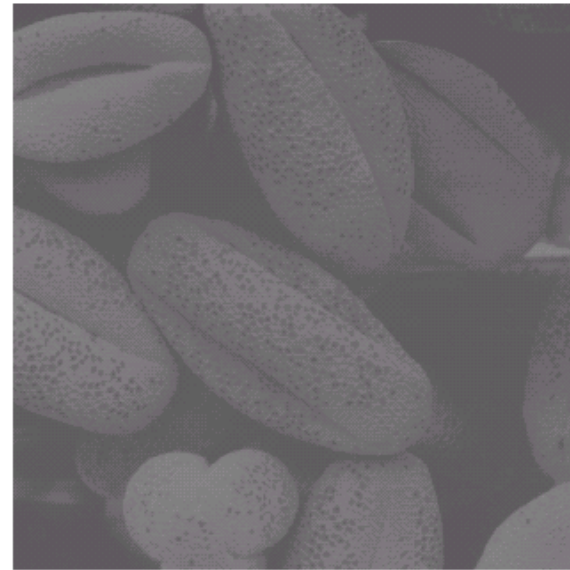
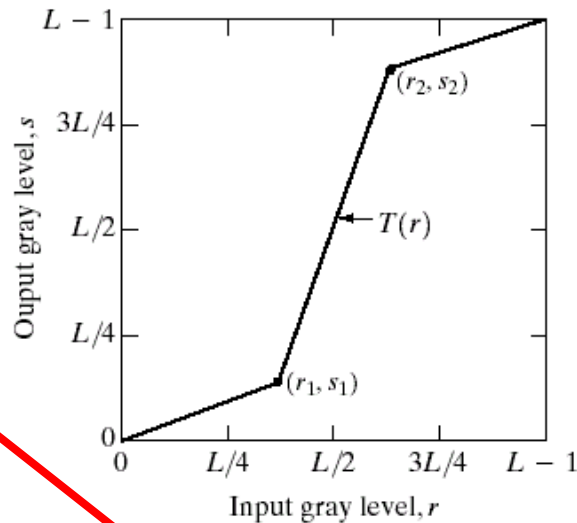
Original/Corrected



**FIGURE 6.36** Color balancing corrections for CMYK color images.

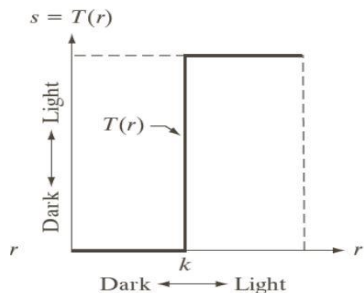
# Gray Level Transformations: Contrast Stretching

It is normally controlled by a **piecewise “linear transformation”**. A special case is the **“thresholding”** when  $r_1=r_2$  and  $s_1=0, s_2=L-1$ .



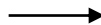
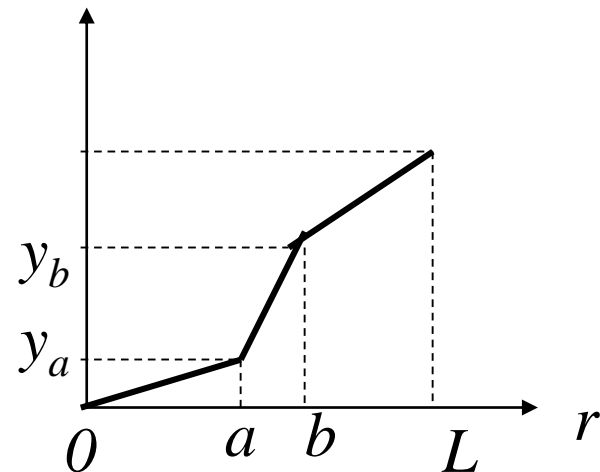
a b  
c d

**FIGURE 3.10**  
Contrast stretching.  
(a) Form of transformation function. (b) A low-contrast image. (c) Result of contrast stretching. (d) Result of thresholding. (Original image courtesy of Dr. Roger Heady, Research School of Biological Sciences, Australian National University, Canberra, Australia.)



# Contrast Stretching

$$T(r) = \begin{cases} \alpha r & 0 \leq r < a \\ \beta(r - a) + y_a & a \leq r < b \\ \gamma(r - b) + y_b & b \leq r < L \end{cases}$$

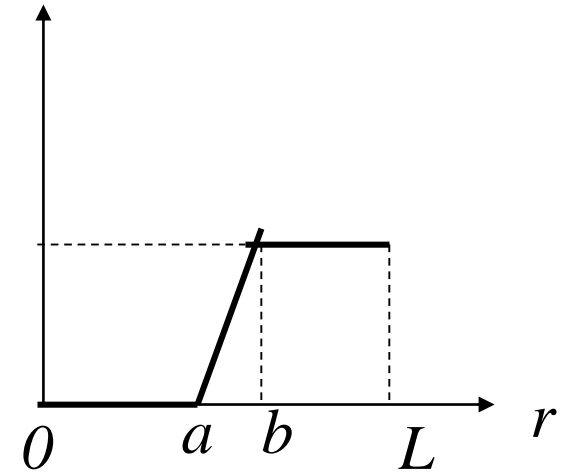


$$a = 50, b = 150, \alpha = 0.2, \beta = 2, \gamma = 1, y_a = 30, y_b = 200$$



# Image Intensity Clipping

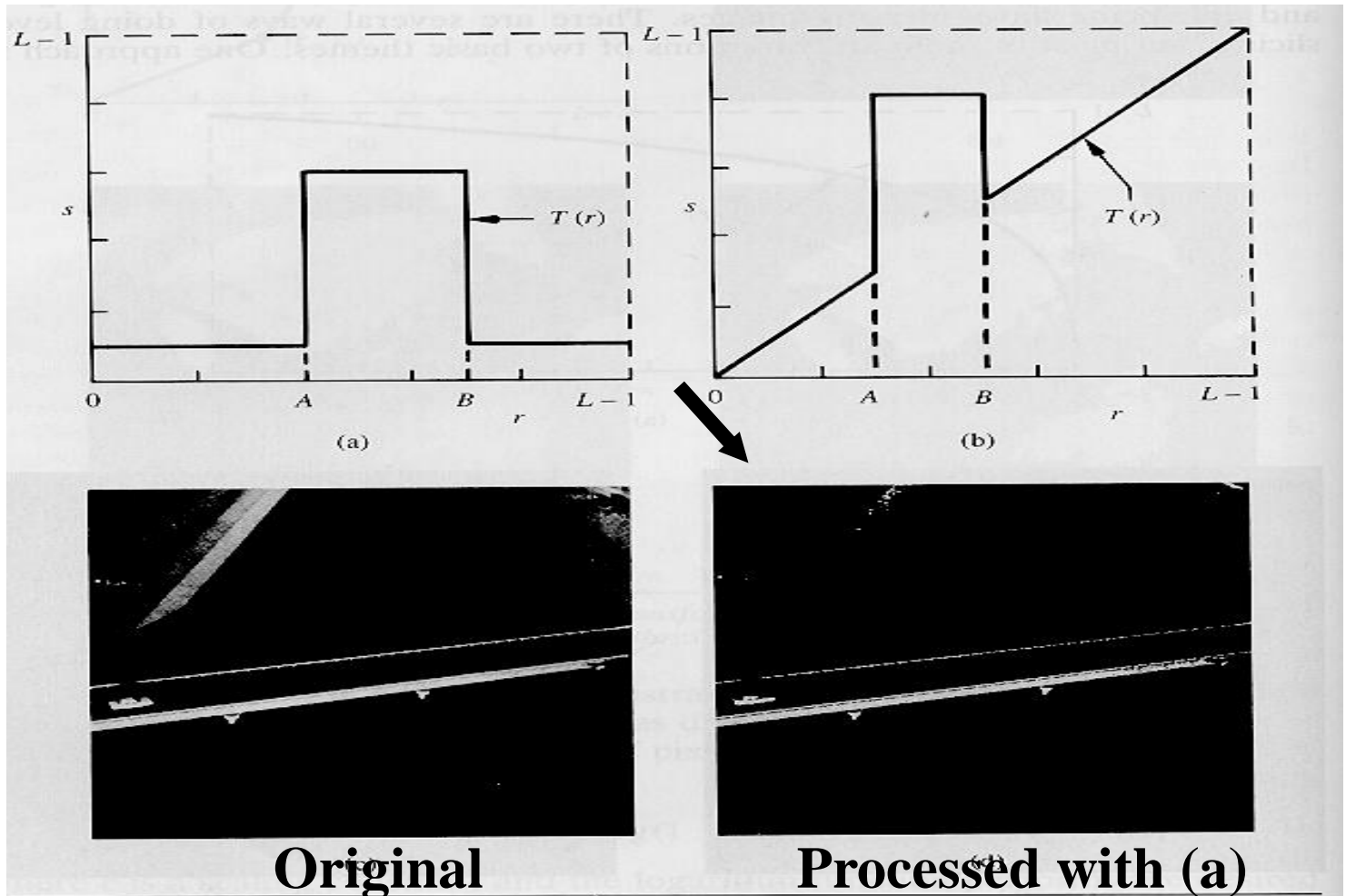
$$T(r) = \begin{cases} 0 & 0 \leq r < a \\ \beta(r-a) & a \leq r < b \\ \beta(r-a) & b \leq r < L \end{cases}$$



$$a = 50, b = 150, \beta = 2$$

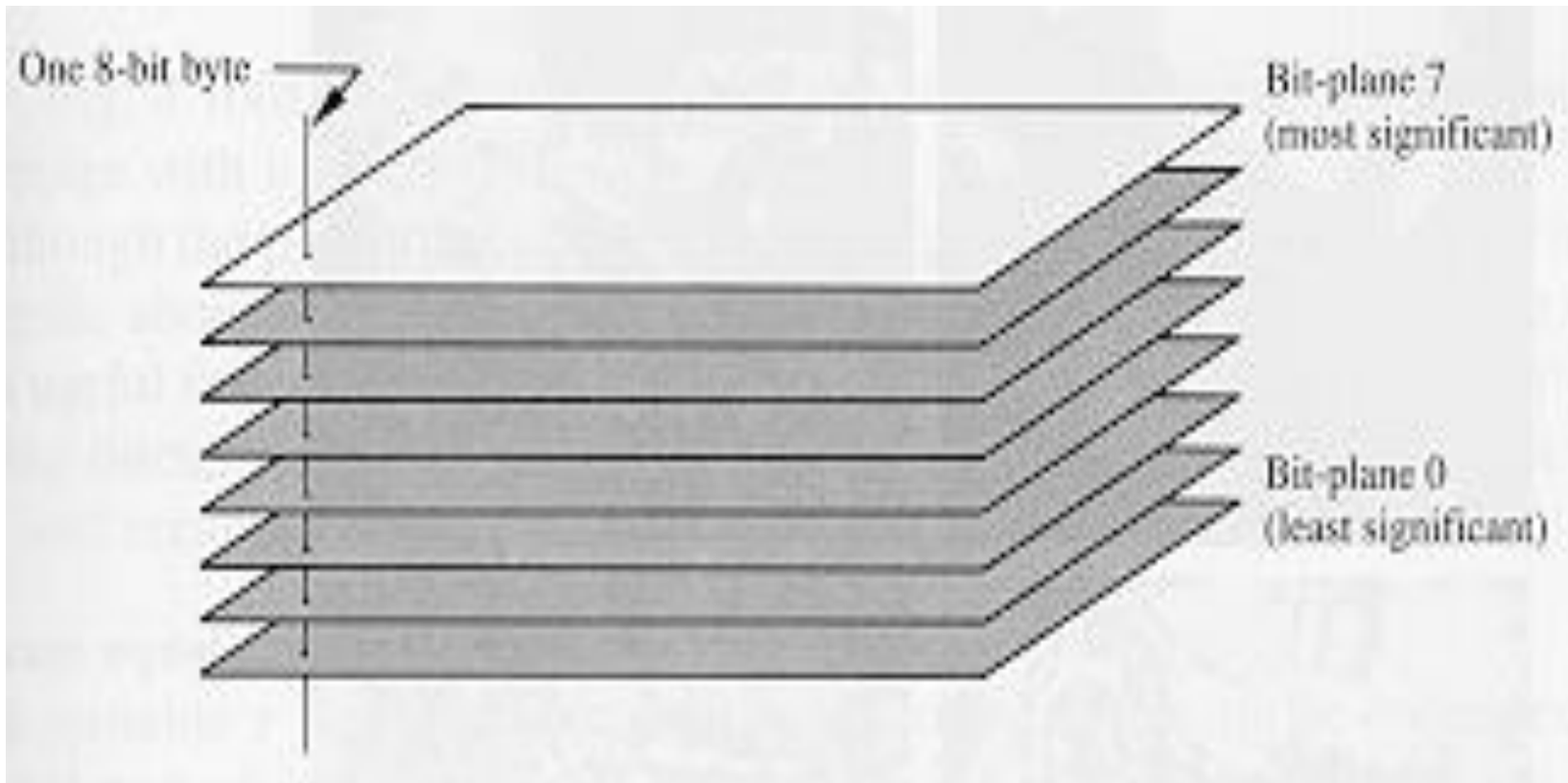
# Point Processing: Gray-Level Slicing

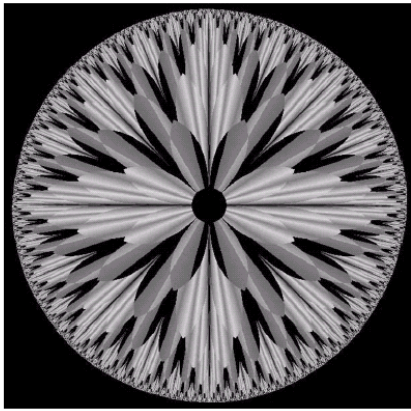
- a) display a “high value” for gray levels of interest and a low value for others,
- b) brighten the desired range of gray levels but preserve the background.



# Point Processing: Bit-Plane Slicing

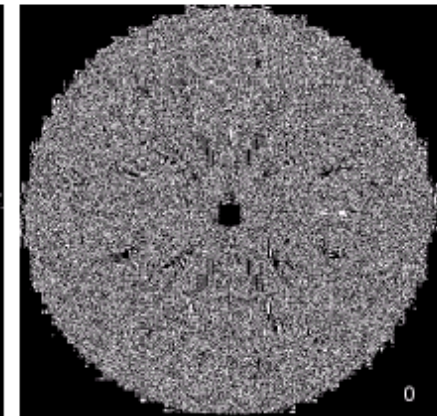
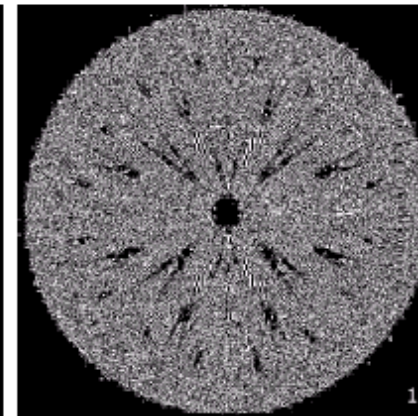
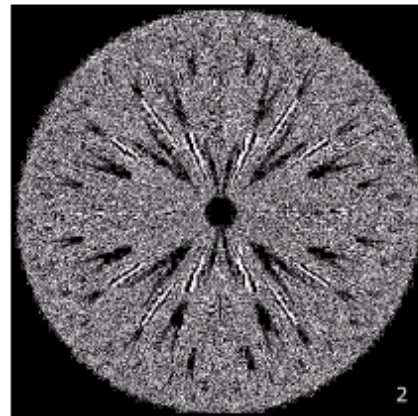
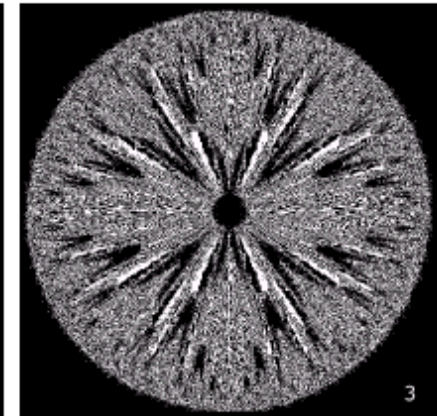
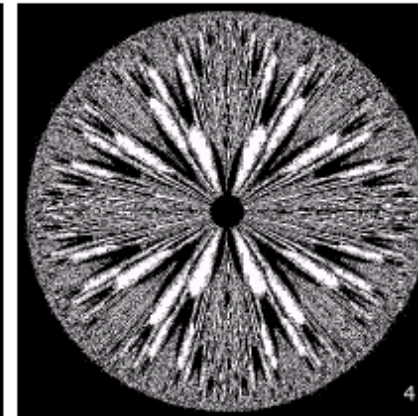
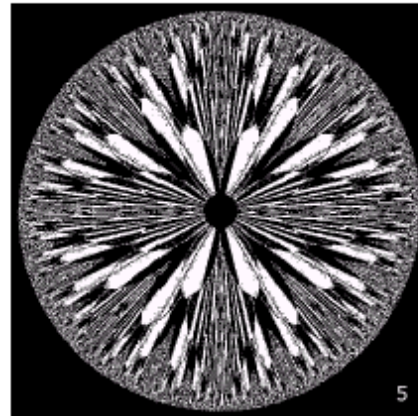
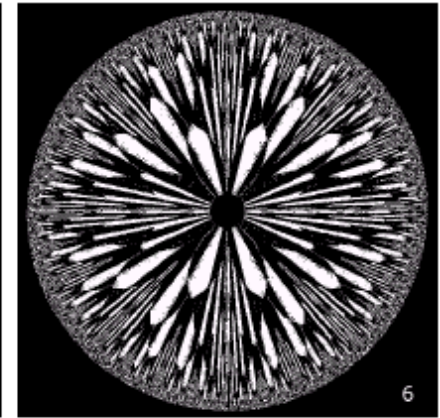
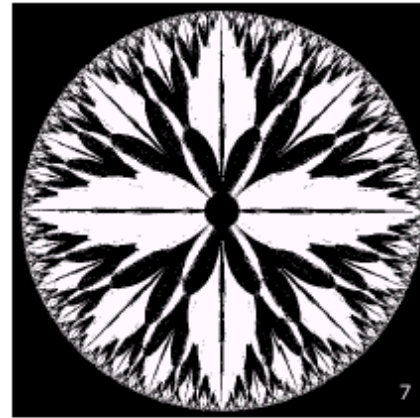
- It highlights the contributions made to the total image appearance by **specific bits**.





**FIGURE 3.13** An 8-bit fractal image. (A fractal is an image generated from  $n$  expressions). (Courtesy of Ms. Melissa D. Binde, Swarthmore College, Swarthmore, MA)

# Point Processing: Bit-Plane Slicing



**FIGURE 3.14** The eight bit planes of the image in Fig. 3.13. The number at the bottom, right of each image identifies the bit plane.



# Point Processing: Bit-Plane Slicing



a	b	c
d	e	f
g	h	i

**FIGURE 3.14** (a) An 8-bit gray-scale image of size  $500 \times 1192$  pixels. (b) through (i) Bit planes 1 through 8, with bit plane 1 corresponding to the least significant bit. Each bit plane is a binary image.

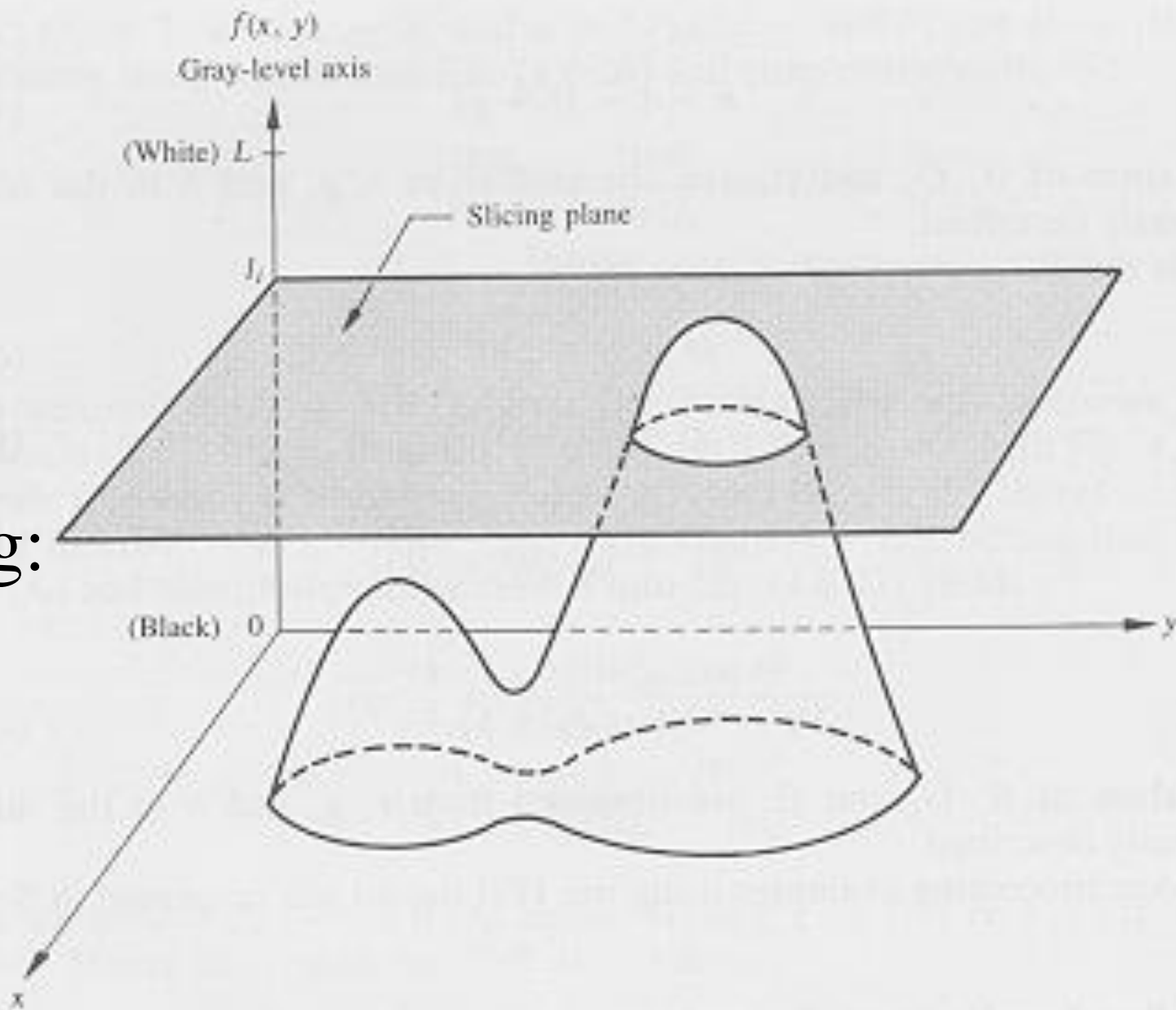
# Combining Bitplanes



a b c

**FIGURE 3.15** Images reconstructed using (a) bit planes 8 and 7; (b) bit planes 8, 7, and 6; and (c) bit planes 8, 7, 6, and 5. Compare (c) with Fig. 3.14(a).

# Pseudo- Color Image Processing: Intensity Slicing



*Figure 4.48 Geometric interpretation of the intensity-slicing technique.*

# Pseudo-Color Image Processing: Intensity Slicing



(a)



(b)

# What is a Histogram?

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- In Statistics, **Histogram** is a graphical representation showing a visual impression of the distribution of data.
- An **Image Histogram** is a type of histogram that acts as a graphical representation of the lightness/color distribution in a digital image. It plots the number of pixels for each value (bin).
- The histogram of a digital image with gray levels in the range  $[0, L-1]$  is a discrete function  $h(r_k) = n_k$ , where  $r_k$  is the  $k$ -th gray level and  $n_k$  is the number of pixels in the image having gray level  $r_k$ .



# Histogram Processing

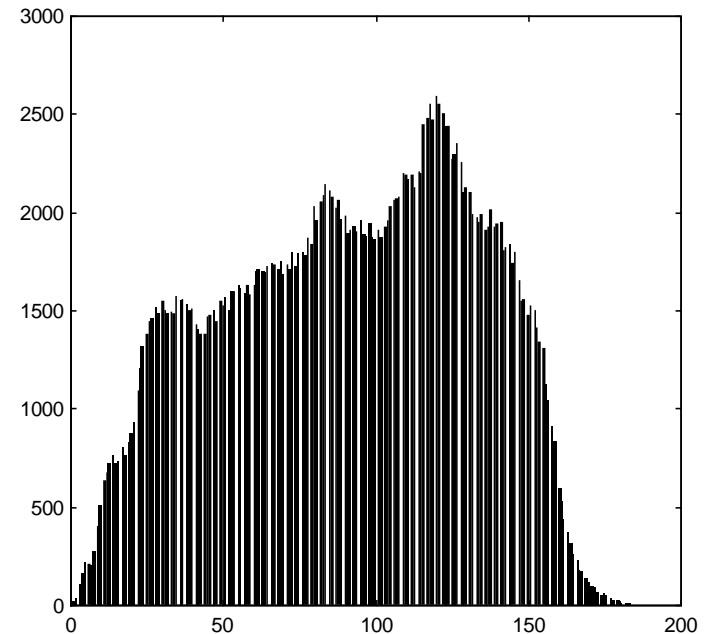
---

- The number of bins can be smaller than the number of gray levels, e.g., **every 4 levels form one bin (256 gray levels, 64 bins)**.
- It is common practice to normalize a histogram by dividing each of its values by the total number of pixels in the image, denoted by  $n$ . Thus, a **normalized histogram** is given by  $p(r_k) = n_k / n$ , for  $k = 0, 1, \dots, L - 1$ .
- Thus,  $p(r_k)$  gives an estimate of the **probability of density (occurrence)** of gray level  $r_k$ . Note that the sum of all components of a normalized histogram is equal to 1.

# Histogram & Probability of Density



MATLAB  
`imhist(x)`



*z*

$r_k$	$n_k$	$p_r(r_k) = n_k/MN$
$r_0 = 0$	790	0.19
$r_1 = 1$	1023	0.25
$r_2 = 2$	850	0.21
$r_3 = 3$	656	0.16
$r_4 = 4$	329	0.08
$r_5 = 5$	245	0.06
$r_6 = 6$	122	0.03
$r_7 = 7$	81	0.02

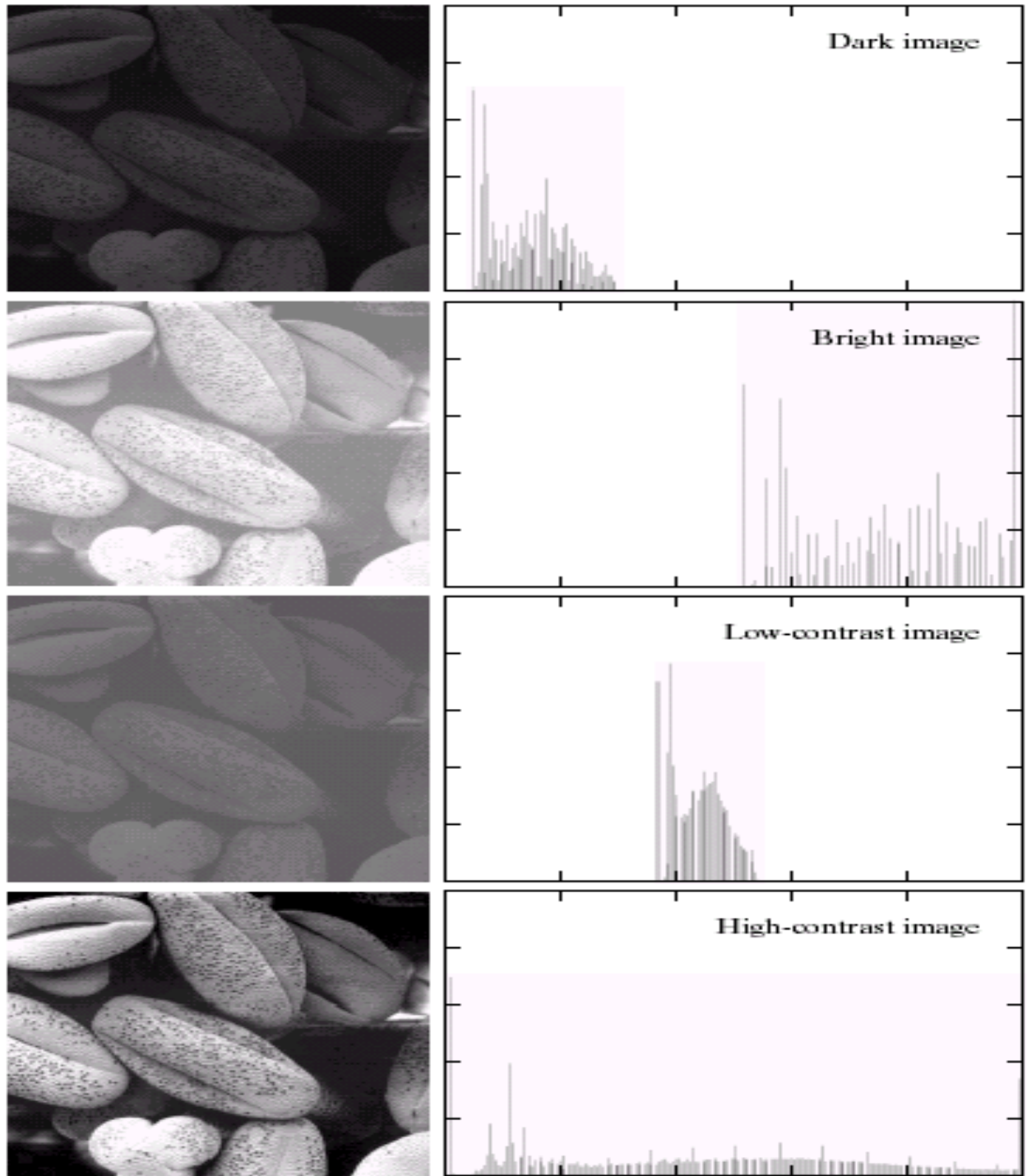
for an M-by-N  
(64x64) image  
size



# Image Histogram

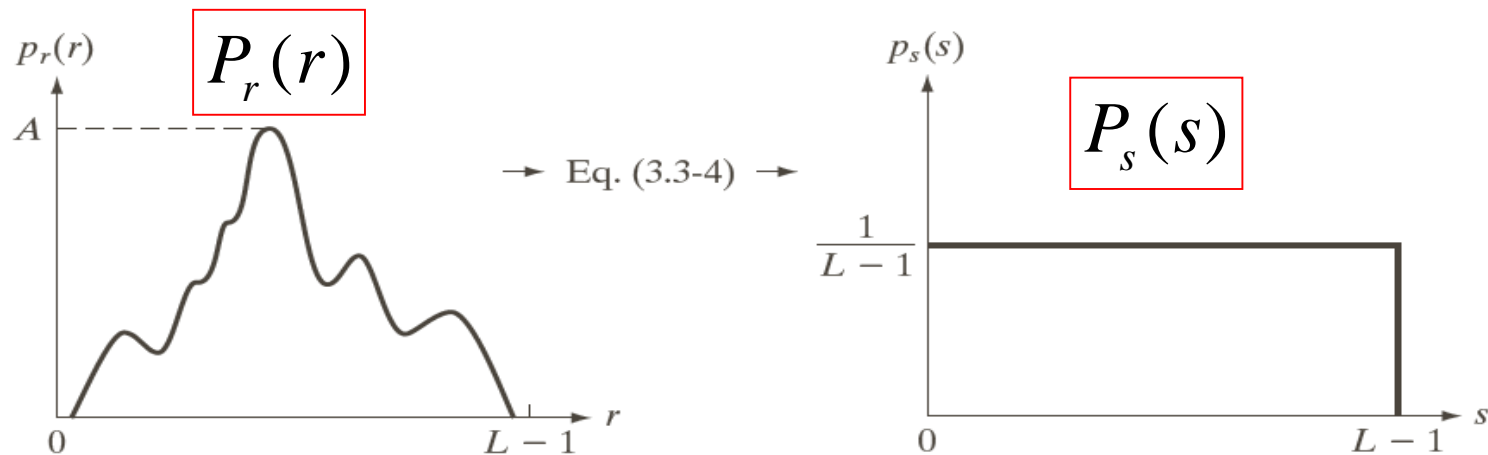
---

Histograms of  
different kinds  
of images



# Histogram Equalization (HE)

- Basic idea: find a map  $T(r)$  such that the histogram (**probability of density, pdf**) of the modified (equalized) image is flat (uniform).



a b

**FIGURE 3.18** (a) An arbitrary PDF. (b) Result of applying the transformation in Eq. (3.3-4) to all intensity levels,  $r$ . The resulting intensities,  $s$ , have a uniform PDF, independently of the form of the PDF of the  $r$ 's.

# Histogram Equalization (HE)

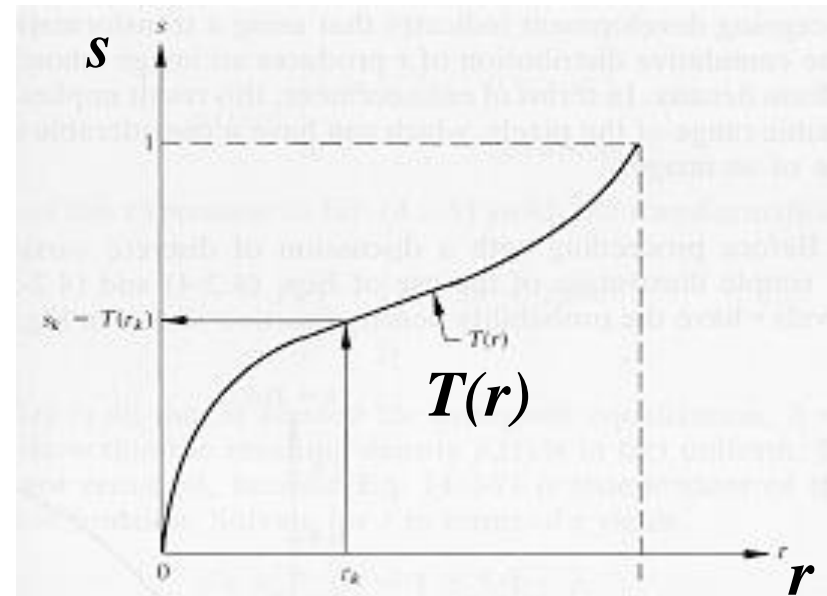
- Key motivation: **cumulative probability function** (cdf) of a random variable approximates a uniform distribution

Suppose  $Pr(k)$  is the histogram (pdf)

$$0 \leq T(r) \leq 1, \quad 0 \leq r \leq 1$$

$$0 \leq T^{-1}(s) \leq 1, \quad 0 \leq s \leq 1$$

$$s = T(r) = \sum_{k=0}^r \text{Pr}(k)$$



# Histogram Equalization

Let  $\frac{ds}{dr} = p_r(r)$ ,  $0 \leq r \leq 1$   $p_r(\cdot)$  is the probability density function.

Then  $s = T(r) = \int_0^r p_r(\omega) d\omega$ .

$$p_s(s) = \left[ p_r(r) \frac{dr}{ds} \right]_{r=T^{-1}(s)} \quad \frac{dr}{ds} = \frac{1}{p_r(r)}$$

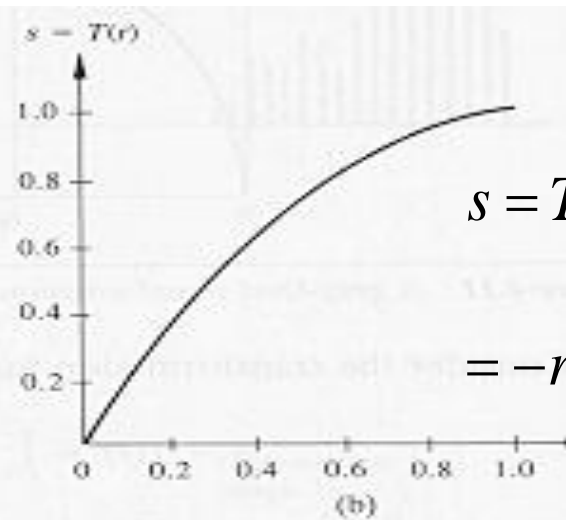
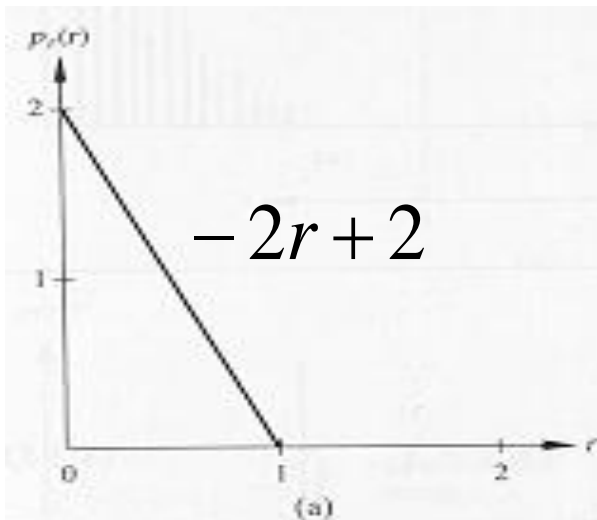
$$\Rightarrow p_s(s) = 1, \quad 0 \leq s \leq 1$$

For digital images,  $r_k$  is discrete:

$$p_r(r_k) = \frac{n_k}{N}$$

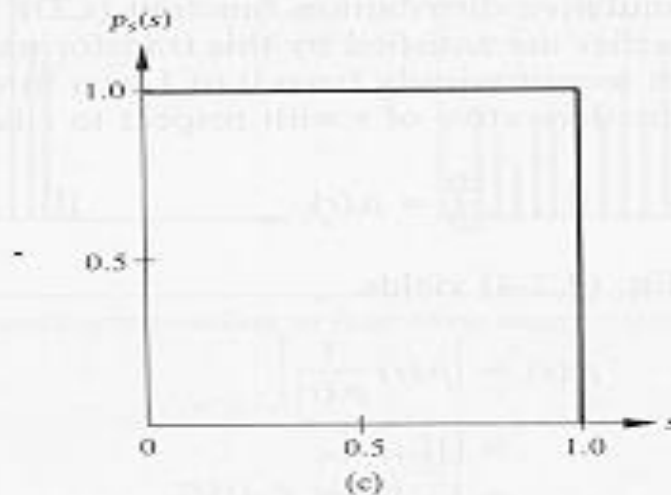
$$s_k = T(r_k) = \sum_{j=0}^k p_r(r_j) = \sum_{j=0}^k \frac{n_j}{N}$$

# Histogram Equalization - Example



$$s = T(r) = \int_0^r (-2w + 2)dw$$

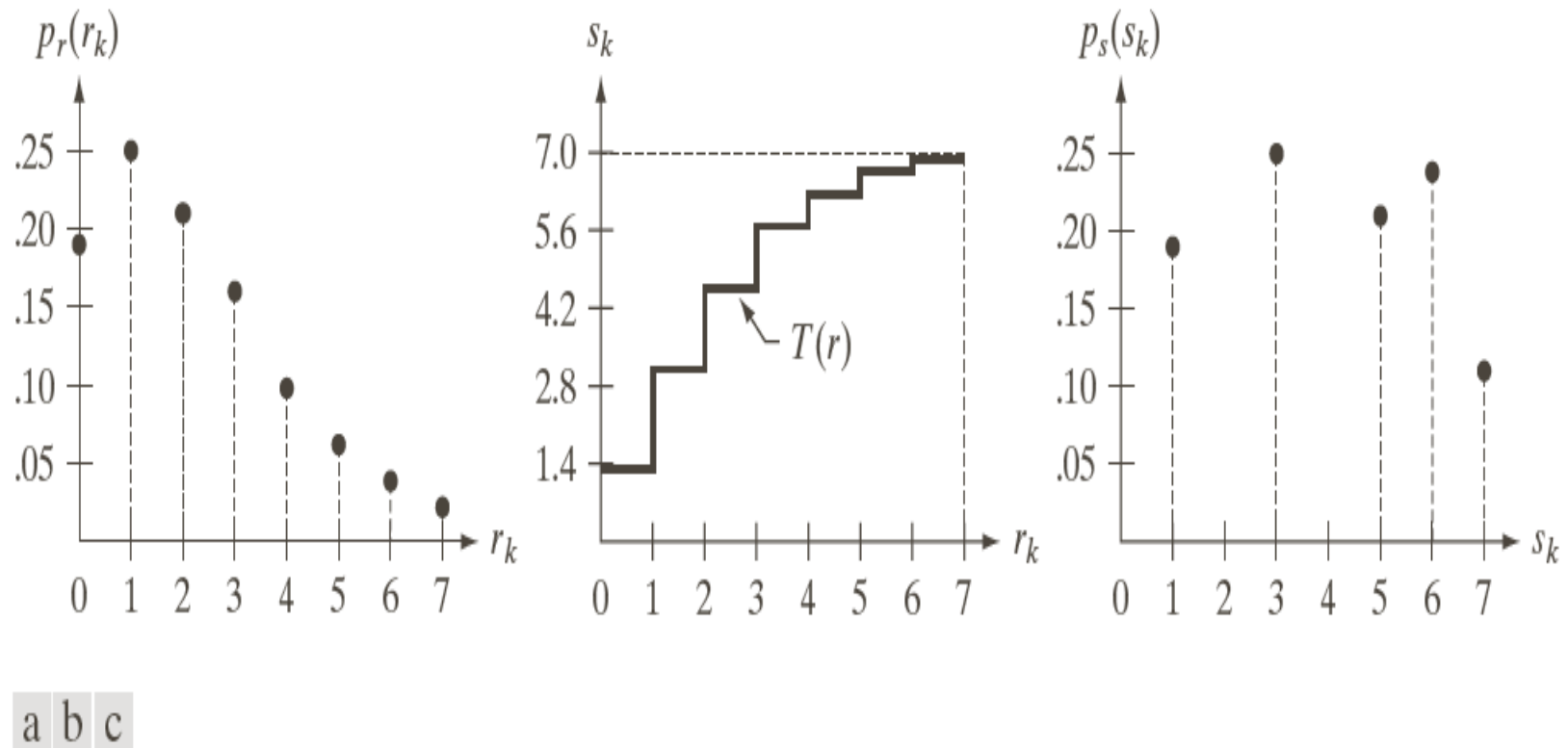
$$= -r^2 + 2r$$



$$r = T^{-1}(s) = 1 - \sqrt{1 - s}$$

$$p_s(s) = \left[ p_r(r) \frac{dr}{ds} \right]_{r=T^{-1}(s)}$$

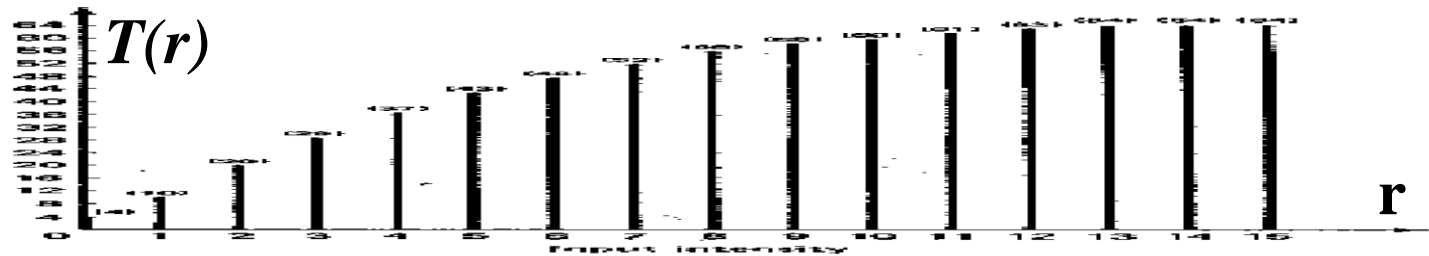
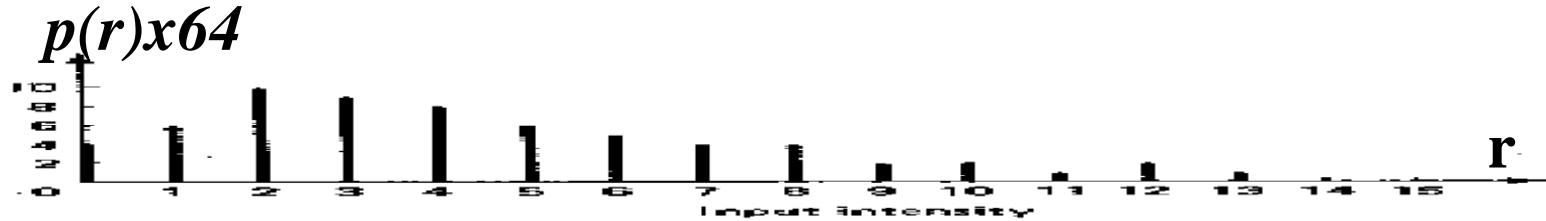
$$= \left[ 2\sqrt{1-s} \frac{d}{ds} (1 - \sqrt{1-s}) \right] = 1$$



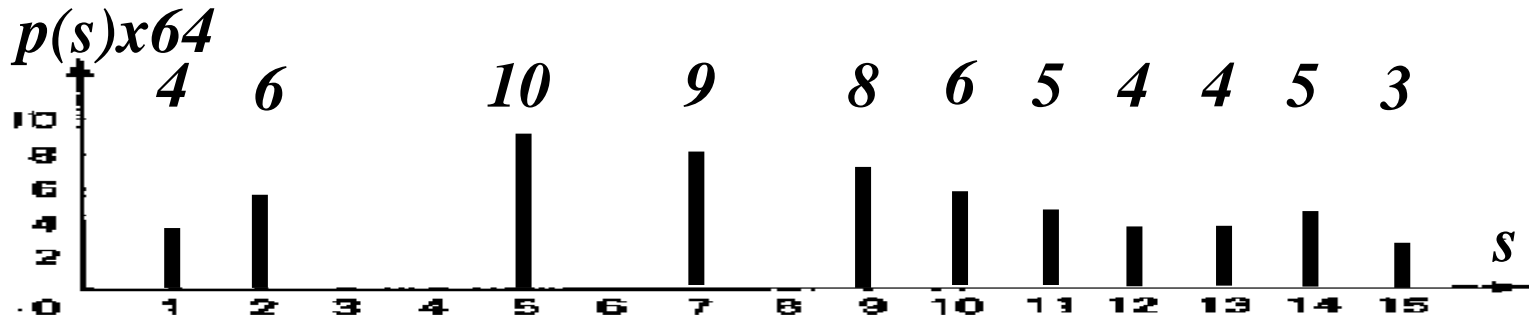
**FIGURE 3.19** Illustration of histogram equalization of a 3-bit (8 intensity levels) image. (a) Original histogram. (b) Transformation function. (c) Equalized histogram.

# An Example of Histogram Equalization

with  $N=64$ ,  $0 \leq r \leq 15$

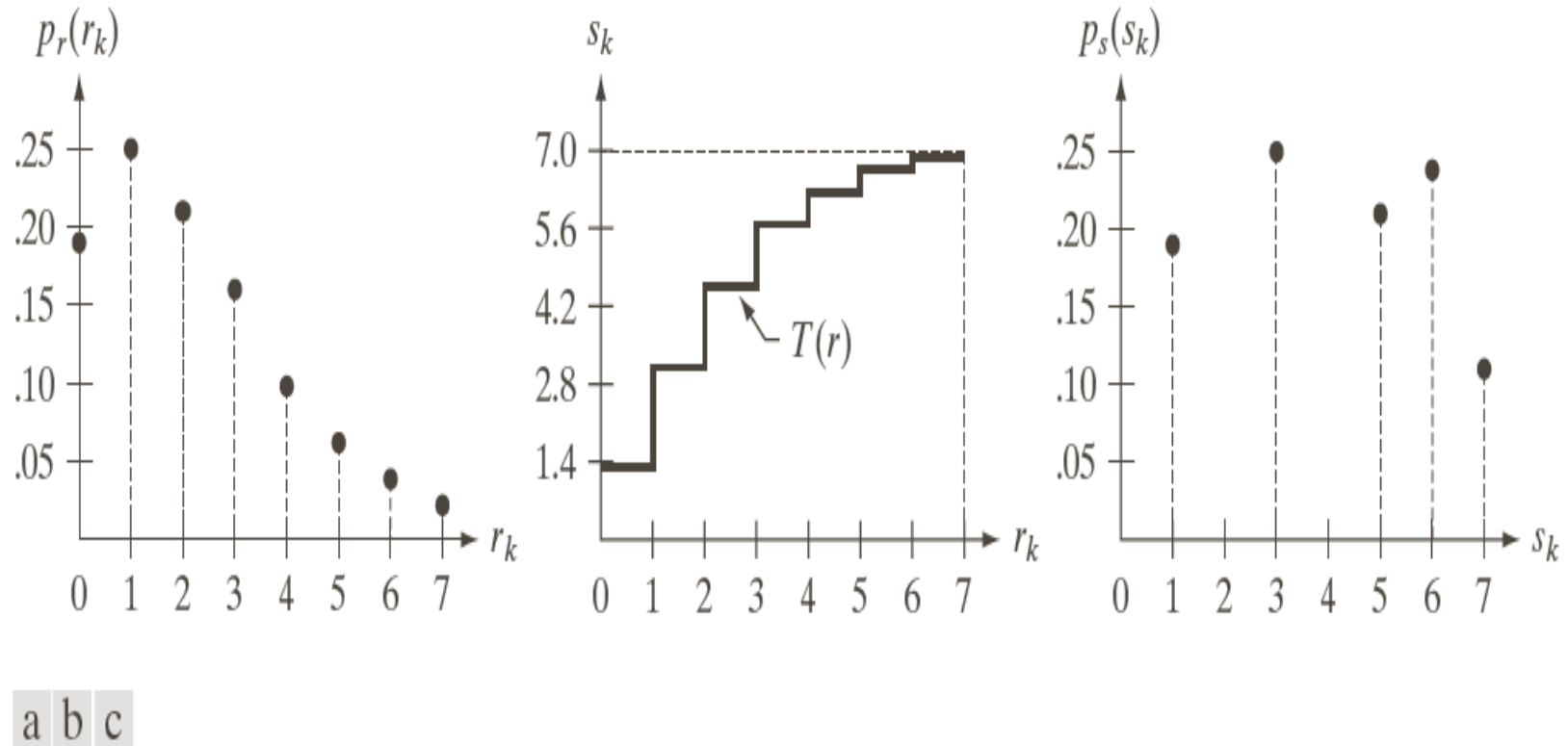


$r$	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
$p(r)x64$	4	6	10	9	8	6	5	4	4	2	2	1	2	1	0	0
$T(r)x64$	4	10	20	29	37	43	48	52	56	58	60	61	63	64	64	64
$s=T(r)x$ <b>15</b>	1	2	5	7	9	10	11	12	13	14	14	14	15	15	15	15





# One More Example

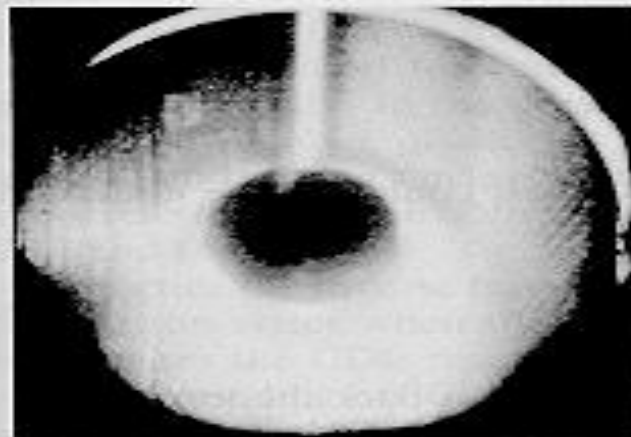
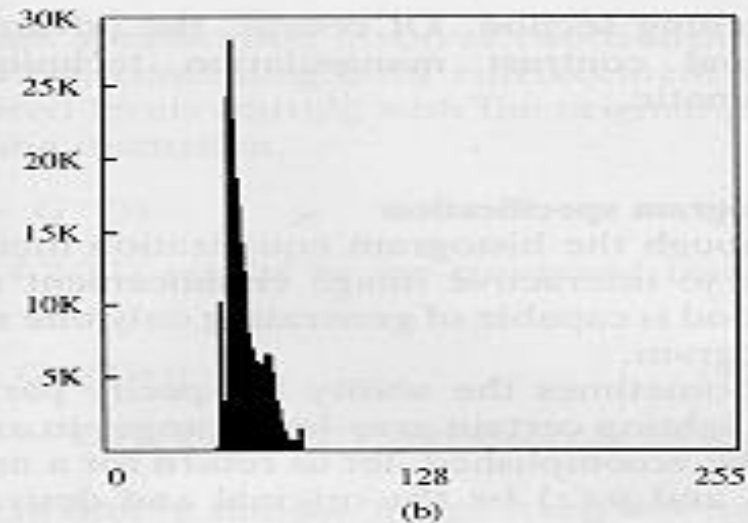


**FIGURE 3.19** Illustration of histogram equalization of a 3-bit (8 intensity levels) image. (a) Original histogram. (b) Transformation function. (c) Equalized histogram.

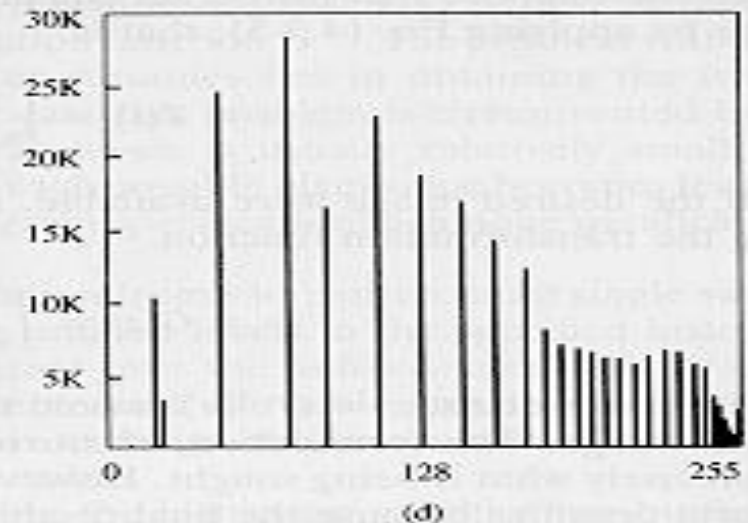
# Histogram Equalization (HE) for Contrast Stretching

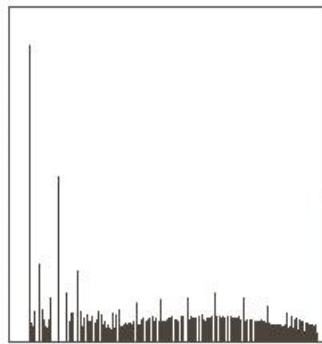
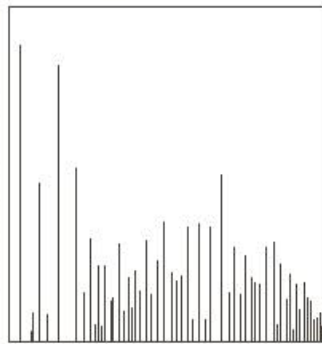
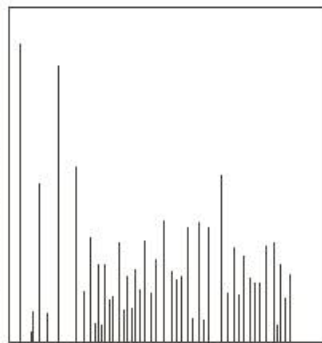
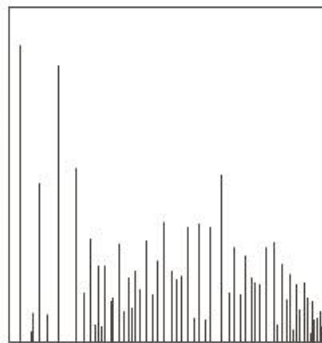


(a)



(c)

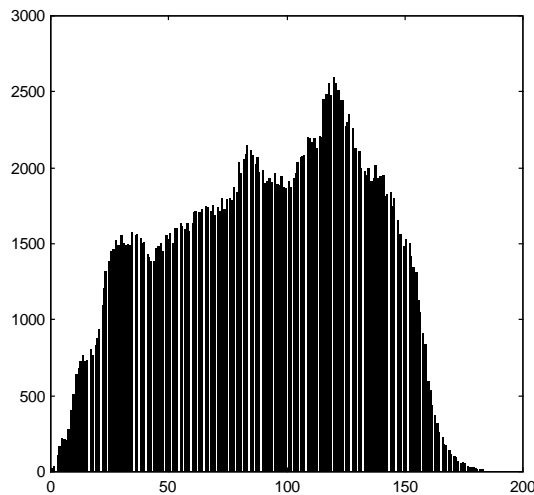




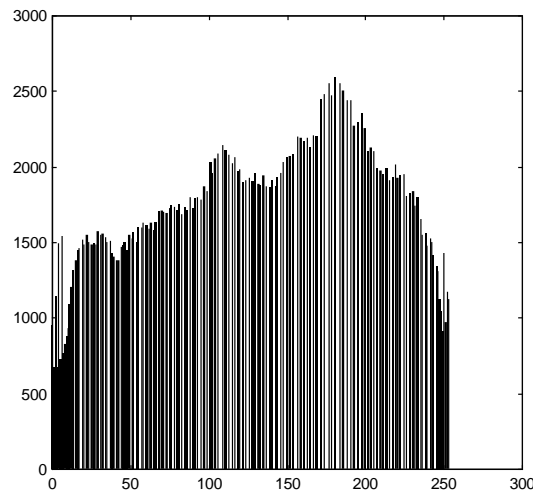
# Another HE Example

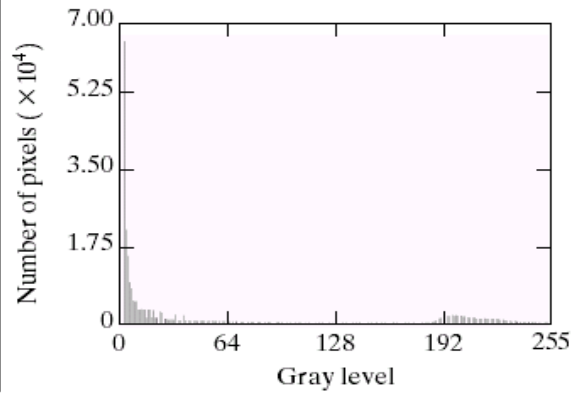
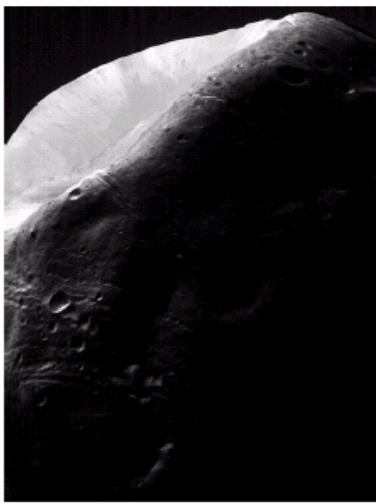


**before**



**after**

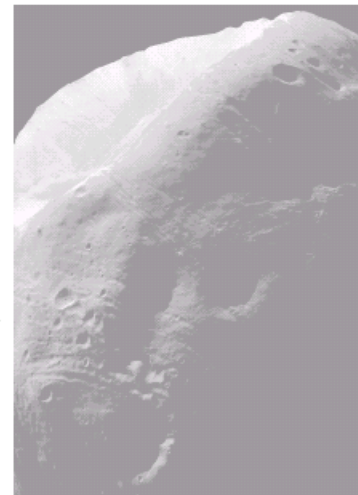
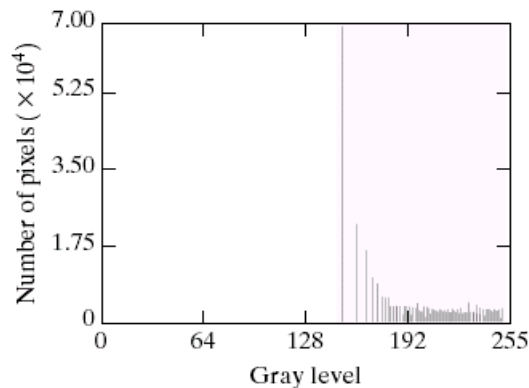
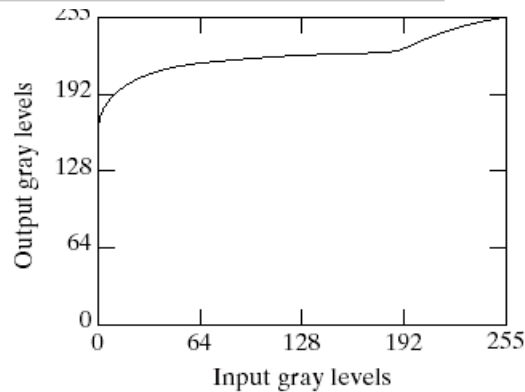




# Example of Histogram Equalization

a b

**FIGURE 3.20** (a) Image of the Mars moon Phobos taken by NASA's *Mars Global Surveyor*. (b) Histogram. (Original image courtesy of NASA.)



a b  
c

**FIGURE 3.21** (a) Transformation function for histogram equalization. (b) Histogram-equalized image (note the washed-out appearance). (c) Histogram of (b).



# Histogram Specification

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- Histogram equalization tries to generate a uniform histogram.
- For interactive image enhancement, the user may like to result in a **customized histogram**.

---> Use Histogram Specification

# Histogram Specification

An image with pixel values  $r$  is to be transformed into an image with a *specified histogram*. Denote the pixel values of the new image as  $u$ . Using histogram equalization, we can *equalize the original and the desired image* to an image with pixel values  $s$  with uniform histogram:

$$s = T(r) = \int_0^r p_r(\omega) d\omega$$

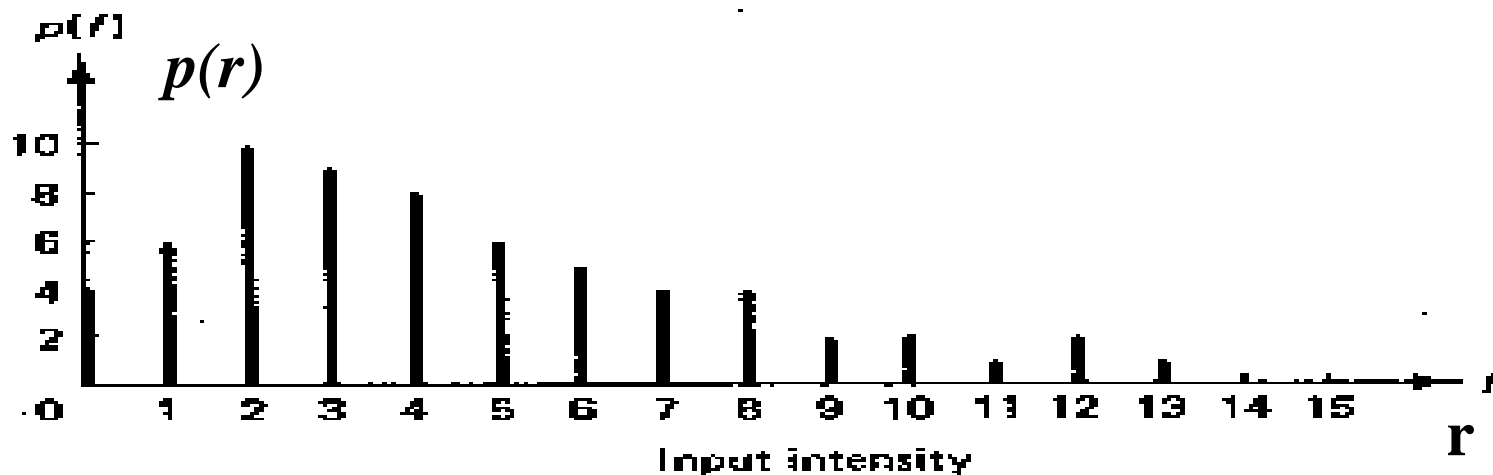
$$s = G(u) = \int_0^u p_u(\omega) d\omega$$

$$u = G^{-1}(s) = G^{-1}(T(r))$$

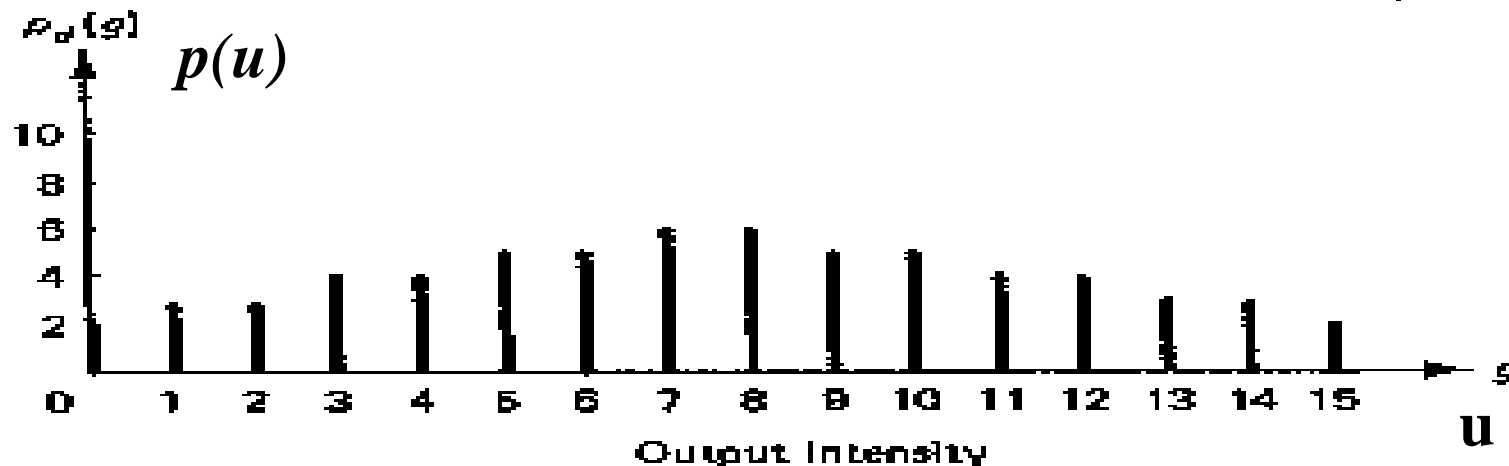
- Specify a particular probability density function  $p(u)$

=>  $G(u)$  => calculate  $G^{-1} T$  for Histogram Specification.

# An Example of Histogram Specification with $N=64$ , $0 \leq r \leq 15$



(a)

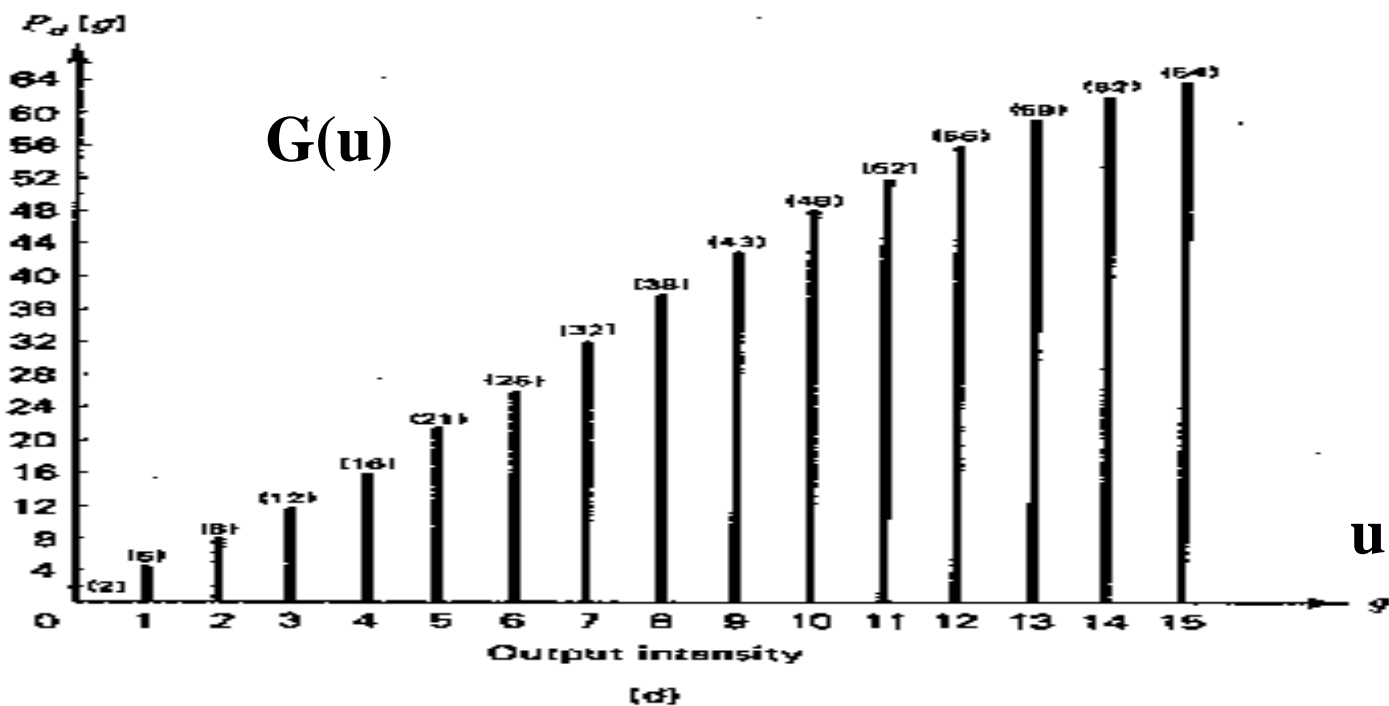
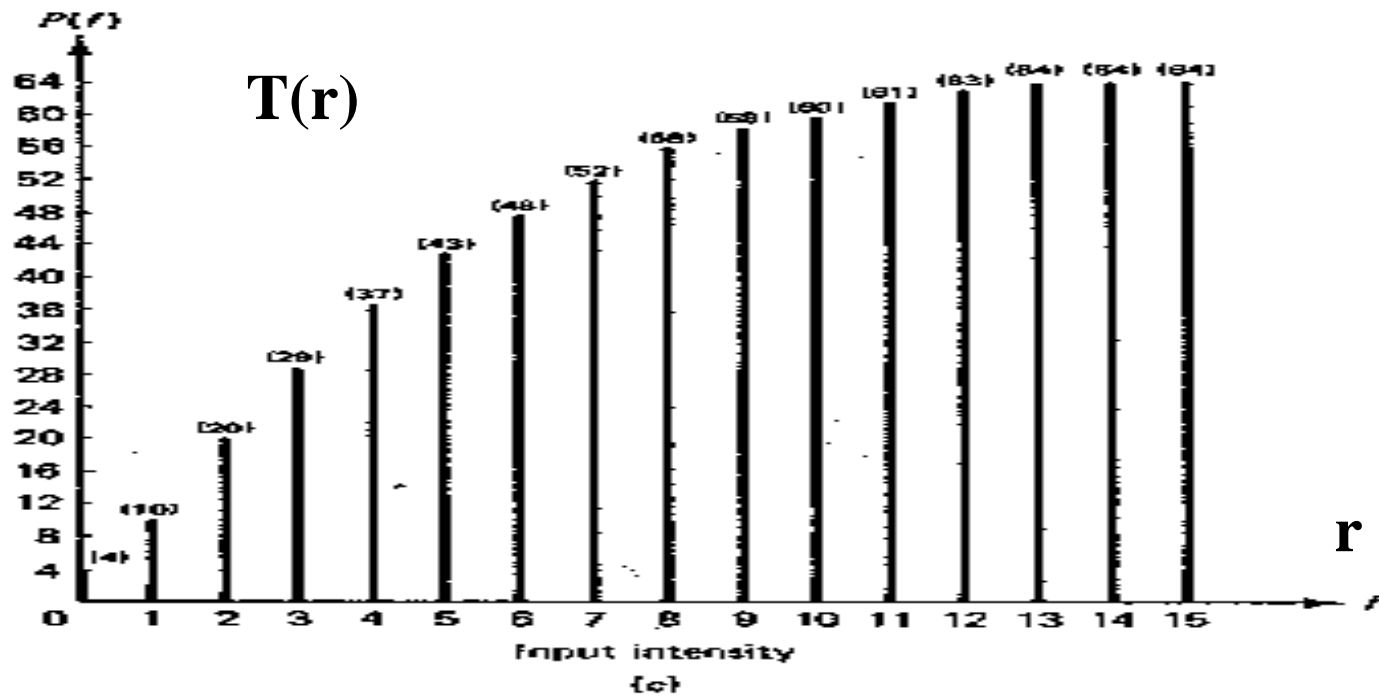


(b)

# An Example of Histogram Specification

with  $N=64$ ,  $0 \leq r \leq 15$

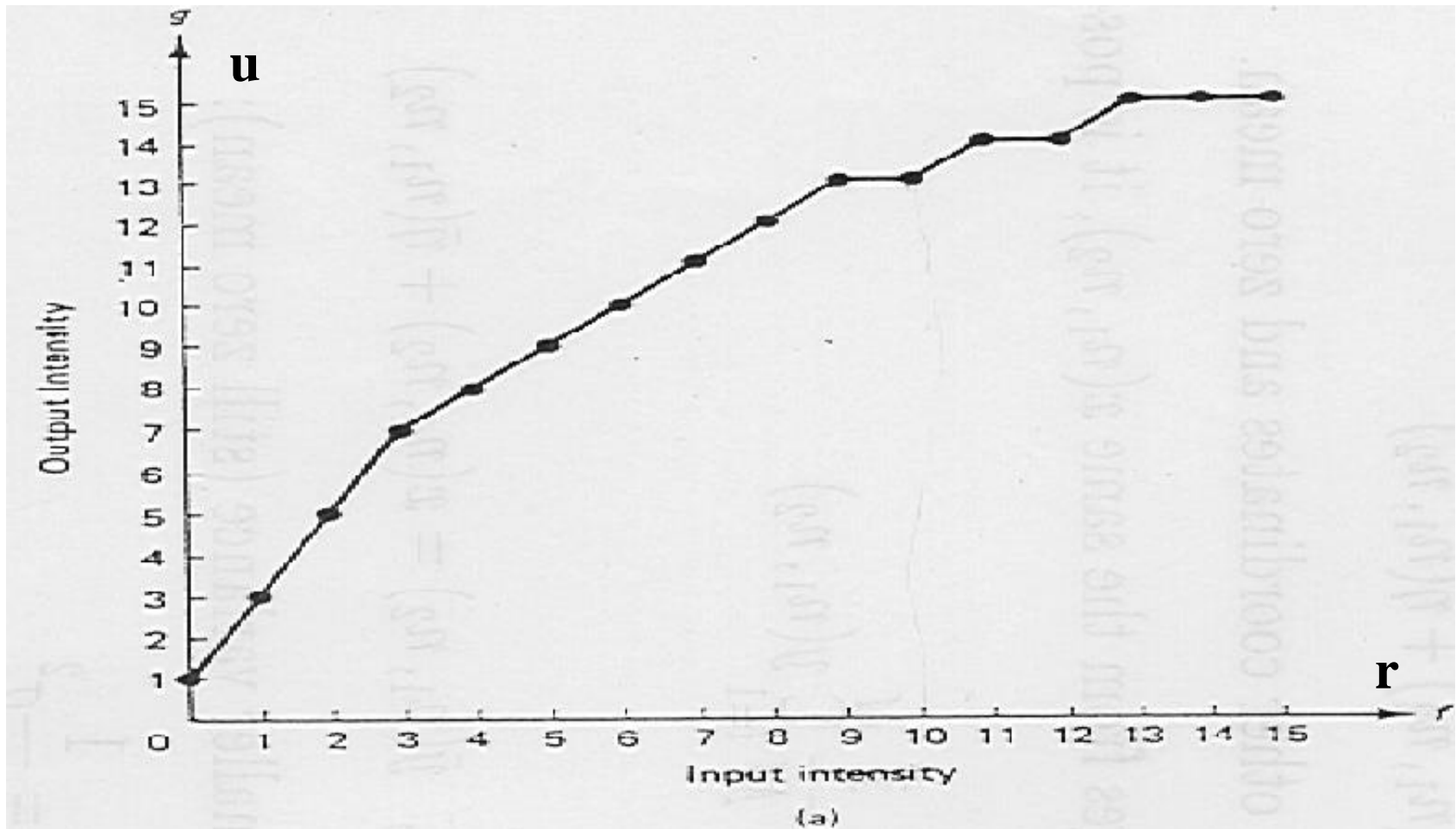
$r$	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
$p(r) \times 64$	4	6	10	9	8	6	5	4	4	2	2	1	2	1	0	0
$T(r) \times 64$	4	10	20	29	37	43	48	52	56	58	60	61	63	64	64	64
$u$	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
$p(u) \times 64$	2	3	3	4	4	5	5	6	6	5	5	4	4	3	3	2
$G(u) \times 64$	2	5	8	12	16	21	26	32	38	43	48	52	56	59	62	64
$r$	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
<u><math>u = G^{-1}(T(r)) \times 15</math></u>	1	3	5	7	8	9	10	11	12	13	13	14	14	15	15	15





# An Example of Histogram Specification with $N=64$ , $0 \leq r \leq 15$ (cot.)

$$u = G^{-1}(T(r))$$

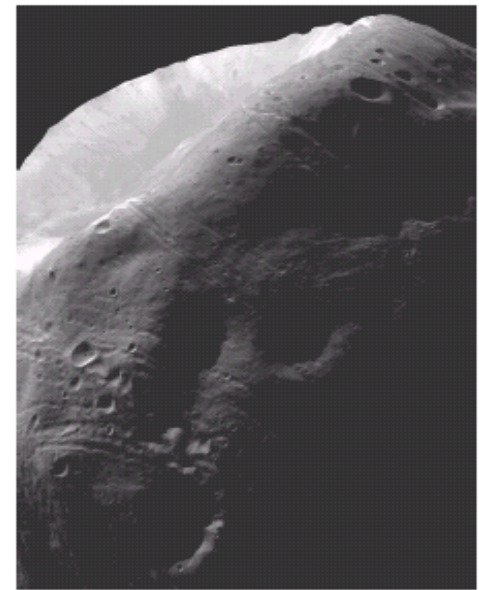
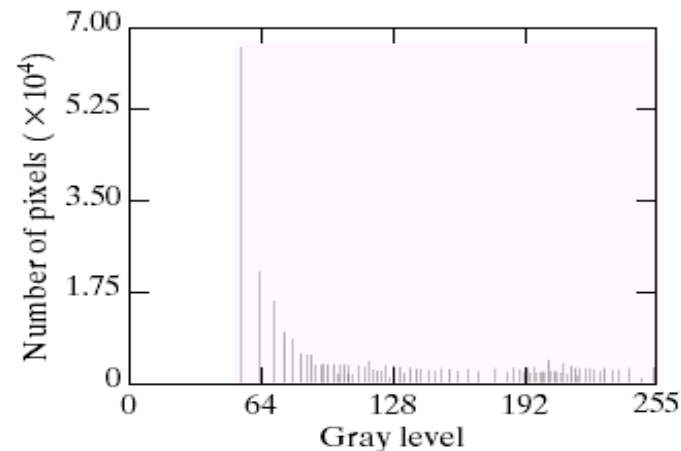
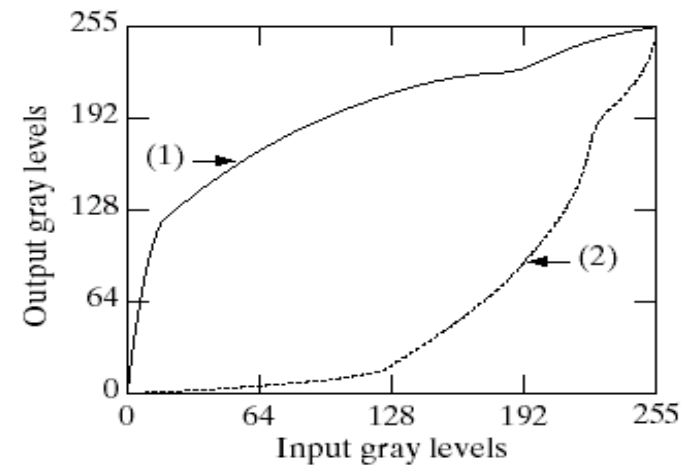
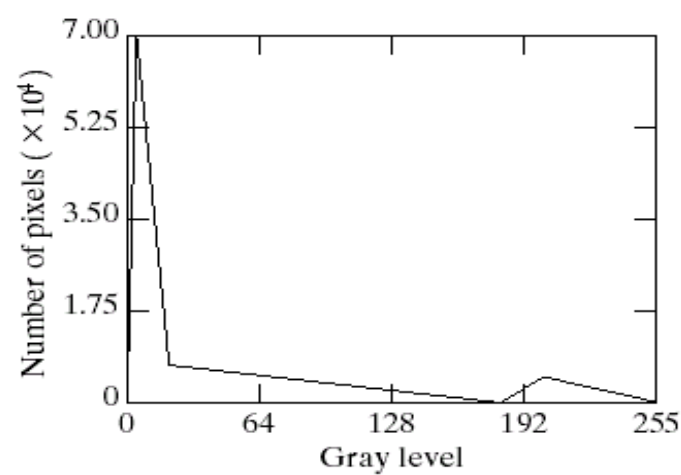


a c  
b  
d

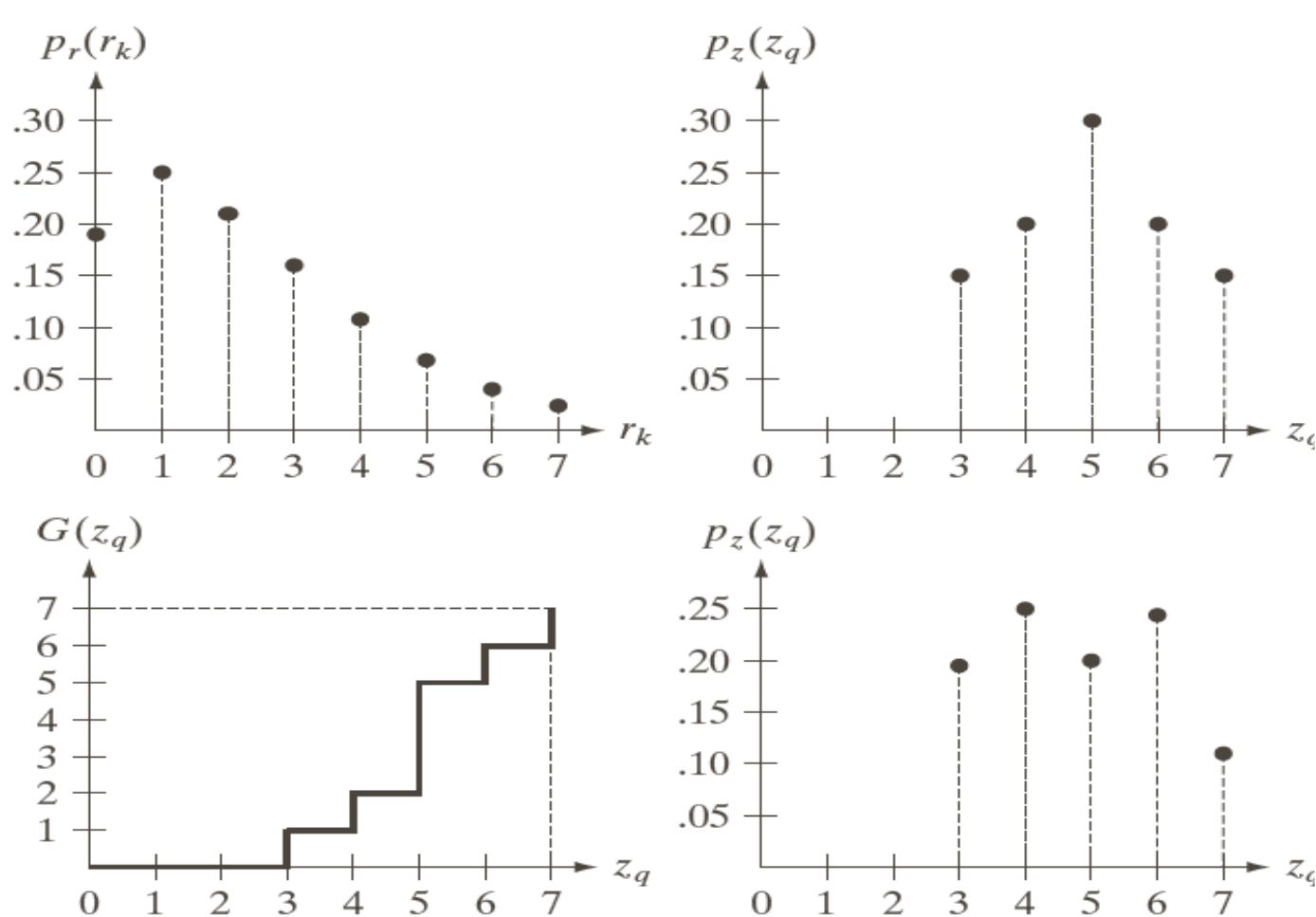
**FIGURE 3.22**

(a) Specified histogram.  
(b) Curve (1) is from Eq. (3.3-14), using the histogram in (a); curve (2) was obtained using the iterative procedure in Eq. (3.3-17).  
(c) Enhanced image using mappings from curve (2).  
(d) Histogram of (c).

## Example of Histogram Specification



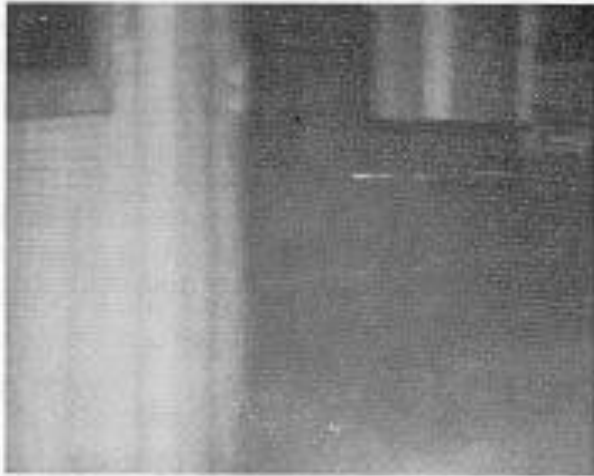
# Another Example of Histogram Specification



**FIGURE 3.22**  
 (a) Histogram of a 3-bit image. (b) Specified histogram. (c) Transformation function obtained from the specified histogram. (d) Result of performing histogram specification. Compare (b) and (d).

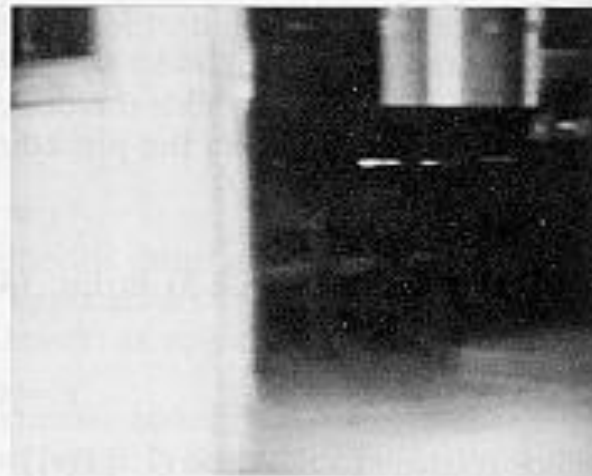
# Example of Histogram Specification

**original**



(a)

**histogram  
equalization**



(b)

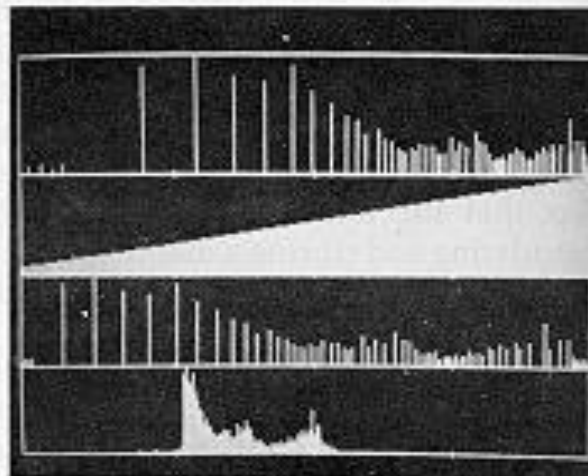
**histograms**

**resulting  
specified  
equalized  
original**

**histogram  
Specifi-  
cation**



(c)



(d)

# Histogram Equalization for Color Picture

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- To apply HE to an RGB color image:

1. Convert RGB to YUV (or HSI/HSV)
2. Apply HE to the Y (or I/V) component
3. Convert back to RGB

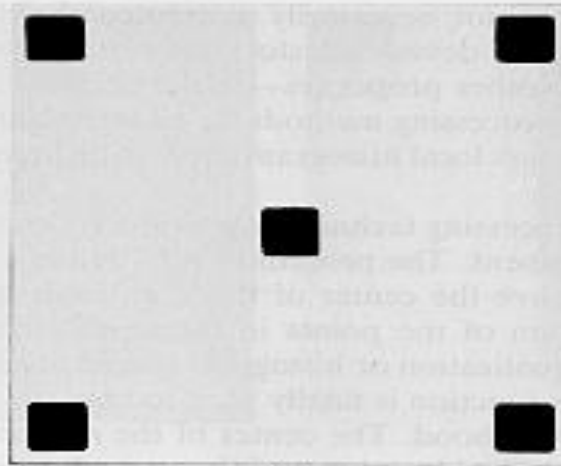
$$\begin{bmatrix} Y \\ U \\ V \end{bmatrix} = \begin{bmatrix} 0.299 & 0.587 & 0.114 \\ -0.147 & -0.289 & 0.436 \\ 0.615 & -0.515 & -0.100 \end{bmatrix} \begin{bmatrix} R \\ G \\ B \end{bmatrix}$$



# Global vs. Local Equalization

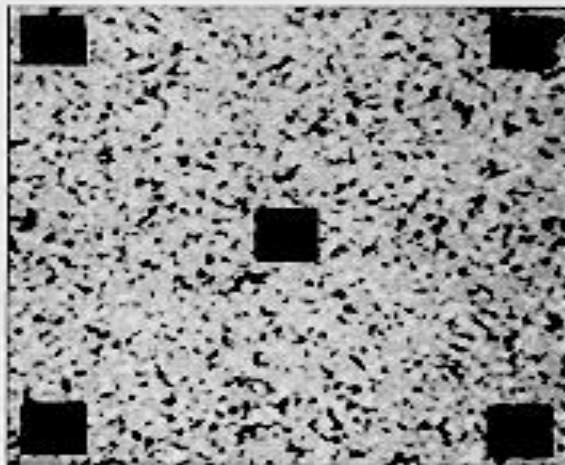
It is possible to do local histogram equalization using a sliding square window.

**Original Image**



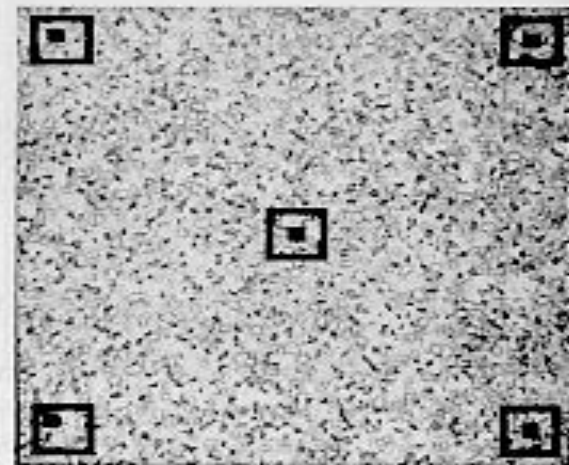
(a)

**Global HE**



(b)

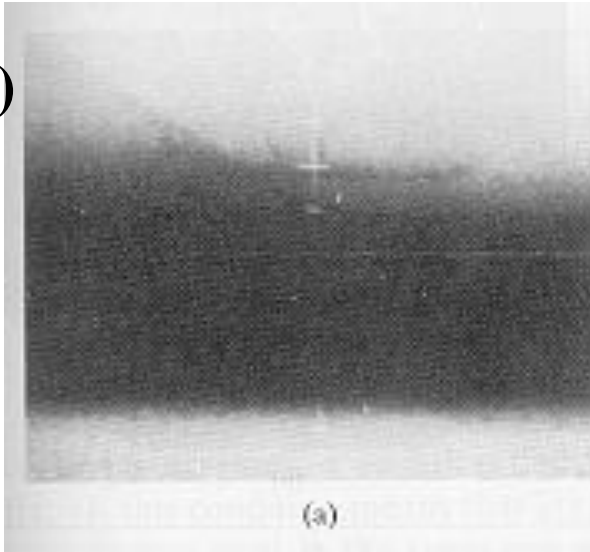
**Local HE (7x7)**



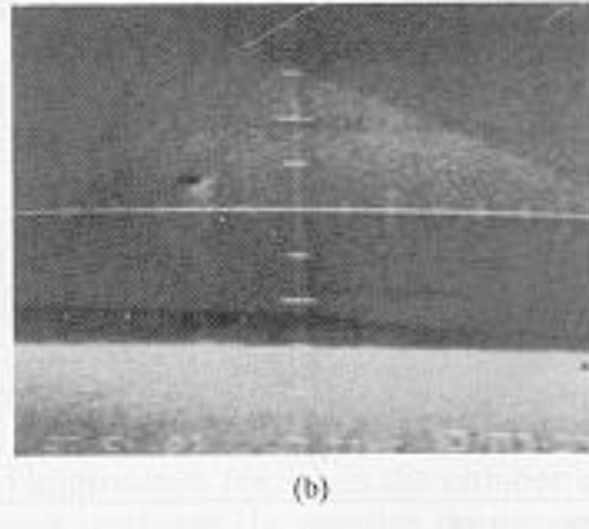
(c)

# Local Enhancement

$f(x,y)$



$g(x,y)$



Using a  
sliding window  
of 15x15 pixels

$$g(x,y) = A(x,y)[f(x,y) - m(x,y)] + m(x,y)$$

$$\text{where } A(x,y) = K \frac{M}{\sigma(x,y)}, \quad 0 < K < 1$$

$$A_{\min} < A(x,y) < A_{\max}$$

$m(x,y)$ : local mean in the window centered at  $(x,y)$

$\sigma(x,y)$ : local standard deviation

$M$ : global mean

# Image Averaging

---

- A **noisy** image  $y(n_1, n_2)$  is created by adding noise  $d(n_1, n_2)$  to an original image  $x(n_1, n_2)$ , i.e.,

$$y(n_1, n_2) = x(n_1, n_2) + d(n_1, n_2)$$

where  $d( )$  is **uncorrelated** and has **zero mean**.

- By averaging a set of noisy images, it is possible to reduce the noise effect.

$$\tilde{y}(n_1, n_2) = \frac{1}{M} \sum_{i=1}^M y(n_1, n_2).$$

$$E[\tilde{y}(n_1, n_2)] = x(n_1, n_2).$$

# Image Averaging

---

$$\tilde{y}(\mathbf{n}_1, \mathbf{n}_2) = x(\mathbf{n}_1, \mathbf{n}_2) + \tilde{d}(\mathbf{n}_1, \mathbf{n}_2)$$

- The new noise  $\tilde{d}(\mathbf{n}_1, \mathbf{n}_2)$  has a smaller variance (still zero mean), i.e.:

$$\sigma_{\tilde{d}}^2 = \frac{1}{M} \sigma_d^2$$



# Noise Reduction by Image Averaging

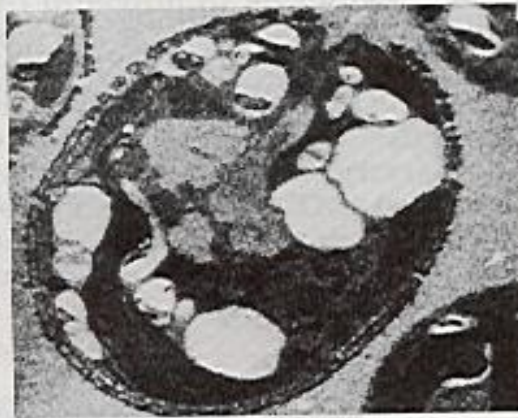
- (a) noisy picture
- (b)-(f): averaging 2, 8, 16, 32, and 128 different noisy images



(a)



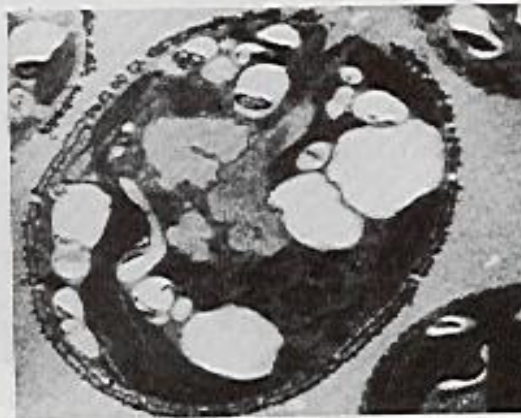
(b)



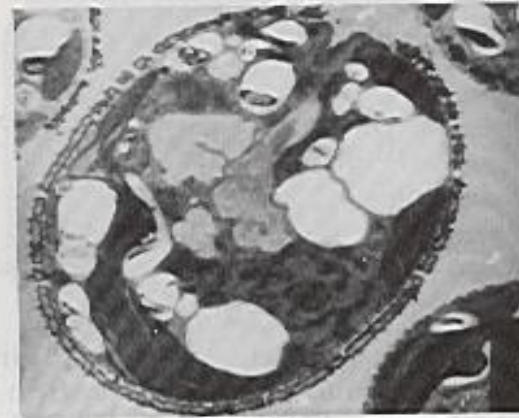
(c)



(d)



(e)



(f)

# Image Manipulation



**Affine Transform**

$$\begin{bmatrix} x' \\ y' \\ 1 \end{bmatrix} = \begin{bmatrix} a & b & e \\ c & d & f \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$

- Translation, scaling, rotation, shearing, reflection, ...

## Translation

$$\begin{bmatrix} x' \\ y' \\ 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & e \\ 0 & 1 & f \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$

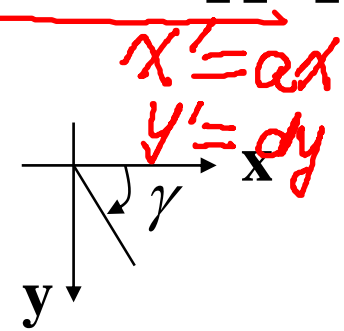
*Handwritten red notes:*  
 $x' = x + e = 2$   
 $y' = y + f = 3$

## Scaling

$$\begin{bmatrix} x' \\ y' \\ 1 \end{bmatrix} = \begin{bmatrix} a & 0 & 0 \\ 0 & d & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$

## Rotation

$$\begin{bmatrix} x' \\ y' \\ 1 \end{bmatrix} = \begin{bmatrix} \cos \gamma & -\sin \gamma & 0 \\ \sin \gamma & \cos \gamma & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$



**These operators can be cascaded by matrix multiplications.**